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Abstract

This paper presents the hysteretic behaviour of three 1/3-scale three-storey steel fibre reinforced concrete (SFRC) coupled shear walls (CSWs) under cyclic loads. The deformation, ductility, energy dissipation, stiffness and crack propagation of the specimens are also discussed and analysed. The results show steel fibre improves the ductility and energy dissipation capacity, and restrains the crack propagation of the CSWs, and delays the degradation of their lateral stiffness and force. Based on the experiments, a simple trilinear model is developed to simulate the skeleton curve of lateral force-displacement of the SFRC CSWs. Through analysing several typical cycles of the hysteretic of these CSWs, the feature points of the proposed hysteretic model are defined which subsequently is used to evaluate the complete hysteretic behaviour of the CSWs. Using existing experimental data and this study, several representative experimental hysteretic cycles are compared with the proposed model. The result indicates a good agreement is reached between the model and experimental results.

Keywords: Steel fibre reinforced concrete; Coupled shear wall; Skeleton curve; Hysteretic model; Seismic assessment;

1. Introduction

Reinforced concrete (RC) coupled shear walls (CSWs) are widely applied in high-rise and multi-storey building systems to provide an effective resistance to horizontal loads such as wind or seismic effects. Fig.1 shows the seismic effects and design method of RC coupled shear wall systems. With the demand of high-rise and multi-storey buildings, it is very significant and necessary to guarantee
that this kind of support elements in building structures can effectively withstand earthquakes without collapses or unrepairable damages. In order to accomplish this goal, RC CSWs usually are designed to possess high lateral resistance strength, excellent deformation, high energy dissipation capacity and stable degradation of post-peak stiffness which all can provide a good control to the horizontal displacement or storey drift of the structures.

A number of experimental studies and numerical analyses have been conducted on RC CSWs in the past four decades (Paulay and Binney 1974; Chaallal and Ghlamallah 1996; Chaallal et al. 1996a; Kuang et al. 1999; Aksogan et al. 2003; Lu and Chen 2005). Based on these studies, several basic design rules, calculation methods, and analytic models had been established. The studies also had mentioned one important fact that the behaviour of coupling systems (mainly coupling beam) greatly affects the structural behaviour of the RC CSWs subjected to seismic effects. These coupling elements usually connect two shear walls in series to transfer the vertical force to get better-distributed load and meet the deformation demands of the structures. This is different with the ones in cantilever shear wall, in which the stiffness, strength, ductility, and dissipating energy of the entire structural system are wholly contingent on the response of the plastic hinge region of the structures. Therefore, the behaviour of coupling beams is very important to the behaviour of CSW system for the elements can distribute effectively the external load effects, rather concentrate the effects on the plastic hinge region of shear walls. However, RC beams is expected to possess stable hysteretic response under reversed loads, a sufficient confinement of concrete in coupling beam and an anchorage of the reinforcements in shear walls should be provided. This often leads to the fact that the coupling beams are designed as a deep beam with heavy reinforcements increasing construction cost and cast inconvenience. In order to improve the resistance behaviour of coupling beams (CBs), many types of CBs have been proposed such as steel CBs (Harries et al. 1993; Park and Yun 2005, 2006; Cheng et al. 2015), concrete-steel composite CBs (Gong and Shahrooz 2001; Harries et al. 2000), concrete

To understand the basic behaviour of RC CSWs using conventional concrete under seismic loads, according to a short review of RC CSWs or RC CBs, several conclusions are drawn:

- The coupling beams in CSW systems have two main beneficial effects: (1) they can reduce the required moment of CSW system comparing with the one in two individual walls; (2) and they can effectively dissipate earthquake energy over the entire height of the walls (Aristizabal-Ocfaoa 1987).

- The three main types of the failure modes of ductile CSWs are: flexural failure of CB, shear failure of CB and rigid action of the CBs in the CSWs, depending on the degree of the interaction and resistance behaviour of the CBs in the system (Subedi 1989);

- The coupling beam at second floor of CSW structures usually yields first and stops resisting lateral deformation of the system;

- The use of diagonal reinforcements is an effective method to enhance the ductility and load resistance capacity of coupling beams. However, the addition of the reinforcement also brings new problems such as cast difficulty of concrete in beam-adjacent wall joint region;

- When CSW systems are subjected to large lateral deformation, most of the lateral force is resisted by the shear walls in the CSWs for the CBs have already undergone the effect of the inelastic deformation and usually failed at that moment;

- The applied axial load of CSWs has a significant influence on the lateral stiffness of the entire structure. Besides, in CSW system, the flexural deformation at the first floor is the highest and decreases along the height of CSW;

- The performance-based seismic designs have only begun to address in fibre reinforced concrete
structural walls. Just limited experimental investigations focused on the seismic response and
damage assessment of the CSW systems to support the development of numerical analysis
method, especially large-scale experimental study;

- According to past experimental and survey studies, when RC CBs have a small shear span
  ratio, their shear failure usually results in that the entire CSW system works as two independent
  individual shear walls. This affects significantly the behaviour of the entire CSW system in
  subsequent seismic loads.

In addition, according to existing experimental studies (Chaallal et al. 1996b; Parra-Montesinos 2005;
Zhang et al. 2007; Canbolat et al. 2005; Zhao and Dun 2014), the use of steel fibre (SF) in RC CBs or
RC shear walls improves the stiffness, ductility and energy dissipation capacity of these members and
enhances their seismic and cracking resistance behaviours as well. However, these studies have just
focused on the effect of steel fibre on individual RC coupling beams or cantilever shear walls such as
the ones reported by our research group (e.g. Zhao and Dun 2014; Zhang 2007). Only a few studies
(Lequesne et al. 2011, 2012; Parra-Montesinos et al. 2017) are available which concerned the
application of fibre in RC CSWs such as the RC shear walls coupled by fibre reinforced concrete
(SFRC) CBs (Lequesne et al. 2011, 2012, Meng 2013) or SFRC CBs (Cai et al. 2016). The research
results illustrated that the use of steel fibre improved the entire deformation and lateral resistance of
the RC CSWs subjected to seismic effects by enhancing the shear resistance, stiffness, energy
dissipation and ductility of CBs. The beams without diagonal steel reinforcements also solve the
congestion of steel rebars in the joint region of the CSW system (Cai et al. 2016). The clear
understanding of the entire behaviour of RC SCWs mainly including co-workability and coupling
effectiveness between RC CBs and shear walls is very significant to their design and application with
the considerations of seismic effects. As a consequence, in order to develop the design methods of
SFRC CSWs and support the development of the performance-based design of CSWs, more
experimental data and analysis models of CSWs are expected.

The main objectives of the current research are to investigate experimentally the seismic hysteretic behaviour of coupled SFRC-CSWs (SFSWs) and to model the skeleton and hysteretic curve of the coupled SFSWs for providing valuable recommendations to their seismic design. To be specific, this paper emphasizes to (a) study the failure modes of SFSWs, deformation and resisting mechanism of various elements of the SFSWs, (b) analyse the ductility, stiffness, and energy dissipation behaviour of the SFSWs, and (c) model the skeleton and hysteretic curves of the elements.

2. Research significance

The study of the application of steel fibres in RC CSWs, one kind of the important support elements in modern earthquake resistance structure systems, is very significant to develop the seismic design method and promote the application of the structures. Unfortunately, just a few studies have been reported focusing on steel fibre RC CSW system. In this study, the seismic response and resistant mechanism of three coupled SFRC-CSWs are experimentally investigated. The skeleton curve and hysteretic behaviour of the specimens are discussed and modelled respectively. Additionally, several key recommendations will be provided to improve the design of CSW system and to propel the establishment of relevant codes for them in the future.

3. Experimental investigation

Test specimens

The experimental program in this study consists of three approximate 1/3–scale three-storey planar RC/SFRC CSWs designed per the Chinese technical specification for the concrete structures of tall buildings JGJ3-2010 (2010), the Chinese code CECS38:2004 (CEC 2004), and the National testing method guideline JGJ101-1996 (CIS 1996). Each CSW specimen has a 3750mm total height and a 1900mm total wall length and includes several wall pieces with 100mm of thickness. The length of
the walls of the CSW system is 600mm with an RC edge column having a width of 400mm and height of 100mm. The sectional size of the coupling beams in each CSW specimen is 500 x 250mm (length x depth) with a span-to-depth ratio of 2.0. In order to avoid the congestion of steel reinforcements, in particular in the zone of the beam-column joints, no diagonal steel reinforcement was used in all coupling beams of the CSW specimens. Fig.2 shows the details of the CSW specimens such as the dimension of various elements and reinforcement arrangement. According to the previous experience in practical engineering and existing literature (Song and Hwang 2004; Singh et al. 2014; Yu et al. 2014; Borg et al. 2016), the usually-used volume fraction of steel fibre in concrete ranges from 0.5% to 2.0%. Tejchman and Kozicki (2010) also reported that the crack load and ultimate load were found to increase with the volume fraction of fibre in concrete. Therefore, the study use two typical volume fractions of steel fibre (1% and 2%) in the specimens. Table.1 lists the details of the main parameters of the test specimens, while their main features are summarized as follow, (a) Specimen SFSW-1—using conventional concrete, as reference specimen; (b) Specimen SFSW-2—using concrete with 1% steel fibre (volume fraction), same reinforcement arrangement as the SFSW-1; (c) Specimen SFSW-3—using concrete with 2% steel fibre (volume fraction), same reinforcement arrangement as the SFSW-1; On the other hand, uniformly distributed longitudinal and transverse steel reinforcements were allocated taking into account the flexural and shear resistance of these elements. The reinforcement arrangements of the CSWs were followed the Chinese code CECS38:2004 (CEC 2004) and the Standard of tall building JGJ3-2010 (CIS 2010). According to the study conducted by Harries (2001), the coupling degree of all CSW specimens are less than 55%. The overall ratios of longitudinal and transverse reinforcements of the shear walls of the three CSW specimens are same, 1.26% and 1.15% respectively. The details of the reinforcements of the coupling beams, base beams and shear walls of
the CSWs are shown in Fig.2. The area ratios of the longitudinal and transverse steel rebars of the
CBs of the CSW specimens are 1.25% and 0.3%, respectively. Besides, a special earthquake report
(EERI 2010) indicated that relatively high levels of axial stress likely led to the great damage suffered
by buildings. However, quite few research (Zhang and Wang 2000; Su et al. 2007) has been reported
about the seismic behaviour of shear walls or CSWs, especially SFRC CSWs. With the increase in the
axial load ratio, the height of concrete spalling rises (Jiang et al 2013). As a start of the experimental
research program of SFRC CSWs and referring to the previous studies (Kabeyasawa and Hiraishi
1998; Gupta and Rangan 1998; Yun et al. 2004; Farvashany et al. 2008; Deng et al. 2008; Jiang et al
2013), a low vertical axial load ($0.1f_{c,eq}$) was used in this study.

Material properties

The compressive strength of used concrete was 40MPa, which was transferred to a mean measure
strength (41.70MPa) of standard cubic ($150\times150\times150\text{ mm}^3$) specimens per the test standard of CECS
13-2009 (CIS 2009). The same concrete with different volume fractions of steel fibre were applied in
the SFSW-2 and SFSW-3 which have a measured cubic compressive strength of 46.44MPa and
50.4MPa, respectively. To avoid the lumping of steel fibre in concrete, steel fibre was first mixed with
coarse aggregates and then mixed slowly with a dry combined mix consisting of cement and fine
aggregates. Once all of the dry mixes have been stirred uniformly, water was then added to make the
steel fibre concretes. Two different types of reinforcing rebars were used in the specimens: plain steel
rebars (HPB 300, $\phi 6$, $\phi 8$ and $\phi 10$) were used for shear walls and coupling beams, and deformed steel
rebars (HRB 400, $\phi 14$ and $\phi 20$) were applied for the base beams. The details of Young’s modulus,
yielding and ultimate strengths of the steel rebars were obtained through relevant Chinese standard
tests. The used steel fibre is a kind of corrugated steel fibres which has an equivalent diameter of
0.76mm, a length of 32mm and a yielding strength of 380MPa provided by the manufacturer,
Instrumentations and testing procedure

The test setup used in this study is shown in Fig.3. Each of specimens was mounted on a strong floor.

A low vertical load (0.1f_{c,c}A_g, about 340kN) was first applied through a combined loading system consisting of four hydraulic vertical jacks, which can move horizontally with the top of the specimens, as the Parts 2-4 shown in Fig.3. A lateral reverse load was then applied to the top beam of the CSW specimens by a horizontal hydraulic jack fixed on a strong reaction wall, as the Part 1 shown in Fig.3.

The reinforcing rebars of the specimens were equipped with several electrical strain gauges to measure their strains, and the deformation of the specimens was monitored by a few Linear Variable Differential Transformers (LVDTs). In the reinforcing rebars of the edge RC columns of the CSWs, 30 strain gauges were used to monitor their strain.

A quasi-static cyclic loading was used at each of specimens and divided clearly into two stages. To observe the crack propagation of each specimen at early stage, a force-control loading (single cyclic for each level) was applied first until the yielding of certain longitudinal reinforcement was observed or when the envelop curve of the force-displacement of the specimen presents an obvious yielding point. At this moment, entire CSW specimen was considered to reach its yielding displacement (\(\Delta_y\)).

Subsequently, to simulate the impacts of earthquake, a series of displacement-control loading cycles (2 cycles for each target level) were applied to each specimen, starting after the specimen reached its yielding displacement (\(\Delta_y\)) and increasing with 0.5\(\Delta_y\) (i.e. 1.5\(\Delta_y\), 2.0\(\Delta_y\), 2.5\(\Delta_y\), 3.0\(\Delta_y\), 3.5\(\Delta_y\), 4.0\(\Delta_y\)).

During the tests, the crack propagation, damage, deformation and lateral force-development of these specimens were recorded and monitored. For the security of test people and equipment, the test is finished if the lateral force of the specimens reduces to 85% of the maximum measured force or the lateral displacement of the specimen reaches about 4 times yielding displacement (4.0\(\Delta_y\)).
4. Test results and analysis

4.1 General behaviour

The main experimental results about the hysteretic behaviour of the specimens are presented in Fig.4. The reference specimen SFSW-1 elastically resists its lateral deformation at the initial stage until the lateral force ($F$) reaches 50kN. At this moment, the first lateral flexural crack was observed on the end of the two walls at the first floor in push loading direction. At the same time, several vertical cracks were confirmed at the ends of CBs in push and pull directions (500-600mm from the ends). The first shear crack was found in the shear walls at the place of 30-150mm from the bottom ends of the first floor shear walls when the lateral load was 125kN (average level in two directions). From 1.0$\Delta_y$ to 3.0$\Delta_y$, the cracks mentioned above developed quickly while a few new cracks appeared, and the concretes at the hinge zones of the CBs and the ends of shear walls were crushed. When the lateral displacement of the reference CSW reached 2.0$\Delta_y$, the specimen presented its maximum strength. When the lateral displacement of the specimen was 4.0$\Delta_y$, although no new crack was observed, more concretes crushing between CBs and shear walls were found or the exposure of some longitudinal steel rebars was confirmed. This severely crushed concrete so that the entire cross-section of the specimen was cut through leading to its structural failure. Like vertical support members such as RC columns, the reverse lateral loading cycles make the RC CSW show an obvious degradation in the lateral resistance force at the later stage.

In the SFRC CSW specimens, similar experimental observations were found in both two specimens at the initial stage, except for the crack propagation of shear walls is slow. The use of SFRC delays the propagation of the flexural and shear cracks in the shear walls and shear-cracks in the coupling beams (see Fig.5). At the same time, the use of steel fibre makes the shear walls get a more uniform stress distribution to resist the external loads uniformly. However, SFRC did not bring an obvious improvement in the resistance of flexural cracks of the coupling beams in the specimens. Besides,
similar damages as the ones in the reference CSW were found in the two SFRC CSWs such as concrete crushing. With regards to the enhancement of CBs caused by the addition of steel fibre, the resistance of shear walls in the SFRC CSWs was higher than the one in the reference RC CSW, which resulted in that the longitudinal steel rebars of the specimens fractured when their lateral displacement was $4.0\Delta_y$.

In the term of hysteretic behaviour, comparing with the reference RC CSW specimen, the SFRC CSW specimens present a plumper hysteretic behaviour with a higher lateral stiffness and stronger bearing capacity and more stable degradation of lateral force at the post-peak stage. In order to understand clearly the crack propagation of the SFRC CSWs, their load cycles were divided into three main stages shown in Fig.4. (1) At the early stage of the loading, most of cracks concentrated and developed quickly at the ends of CBs because of the large deformation caused by a strong bending moment at the top of shear walls. This fits well with the design of these specimens in this study. In the SFRC CSWs, however, the use of steel fibre makes these CBs present a relative slower crack propagation. (2) At middle stage of the loading, many lateral flexural cracks propagated in the two shear walls of the SFRC CSWs. However, the reference RC CSW resisted the propagation of the cracks through the action of longitudinal reinforcements until the cracks occurred in the upper part of shear wall. But steel fibre improved the cracking resistance of the shear walls making the entire CSW present more uniform stress situation. (3) After the coupling beams of CSWs stopped working due to more and wider interfacial cut-through cracks, the crack propagation of the entire CSWs focused on the ends of the shear walls. The cracks widened sharply at the below end of the wall leading to more concrete crushing. A few flexural-shear cracks occurred at the shear walls at each floor meaning the steel fibre provided a good restriction to the horizontal flexural cracks.

The failure of all specimens were flexural-dominant failure model. This indicates the design of the
CSWs per the Chinese code JGJ 3-2010 (CIS 2010) is acceptable. The use of steel fibre has a significant influence on the crack propagation and deformation of the CSW specimens, including control of the number of crack and uniformly distribution of these cracks. Besides, the crushing of concrete at the joint zone between shear walls and CBs was lightened, as shown in Fig.5.

4.2 Deformation mechanism of RC/SFRC CSWs

(1) Deformation of shear walls

The deformation situation of shear wall is helpful to understand the transfer mechanism of external loads in CSW system. As shown in Fig.6, main experimental observations were drawn as,

- a. The longitudinal reinforcements located at the critical sections such as the ends of shear walls presented their highest strain levels in all tested CSW specimens.
- b. According to the test results, the deformation of the reinforcements at the ends of the RC CSW present a considerable elastic feature, even when the lateral resistance force of the CSW decreases at the later stage. This is explained by the fact that the entire CSW system can be switched into two single shear walls after the CBs stopped working at large deformation stage. When steel fibre was used in RC CSWs, the lateral resistance and deformation of CBs were improved enhancing the lateral deformation capacity of the entire CSW system.
- c. The use of steel fibre makes the CSW system obtain a more uniform stress distribution by controlling the deformation and damage of the end zones of shear walls and transferring the stress to the reinforcements of the walls at above floors. This was verified by the fact that the strain of longitudinal reinforcements in the RC CSW was smaller than the one in SFRC-CSWs at the second and third floor.
- d. Because of the additional confinement effect of the top RC columns on the third floor of SFRC CSWs, the strain of reinforcements at the third floor is usually higher than the one at the
second floor. However, these reinforcements still did not reach their yielding strengths. It should be noted that the top loading beam also serves to restrain axial forces in the beams and improve the behaviour of entire CSW for it was cast integrally with the shear walls. For this, all specimens exhibit a classic single large crack appearing at the ends of the beams. Similar to the results reported by Paulay (1971), this leads to sliding shear failures, particularly where tensile forces are developed in the beams.

e. After some longitudinal reinforcements of the shear walls in SFRC CSWs reach their ultimate strengths, for the walls still needed to resist the lateral deformation, the strains of the reinforcements in the upper floors increased (see Fig.6).

(2) Deformation of coupling beams in CSWs

The strains of the reinforcements of the CBs in the reference RC CSW are usually less than the ones in SFRC CSWs. It is attributed to that the large crushed concrete cover in RC coupling beams makes the beams to stop providing an effective coupling action for the deformation of the two shear walls. In the SFRC CSWs, however, the use of steel fibre improves the coupling action of CBs which makes the strains of the reinforcements in these SFRC CSWs obtain a continuous increase.

Based on above analysis, it was found that steel fibres can effectively enhance the shear resistance of CBs which enhances the deformability of the entire CSW system, and can reduce the concrete crushing in the hinge zones of the CBs which ensures their coupling action at later stage. These make the CBs in SFRC CSWs more effective to resist the reverse seismic loads of the entire behaviour of the structure. This is also helpful to control the degradation of lateral stiffness and to improve the lateral resistance force, energy dissipation of the CSW systems.

4.3 Seismic response—Ductility, stiffness and energy dissipation
Ductility, stiffness and energy dissipation capacity are important assessment indexes to evaluate the seismic response of RC structural members. A high level of ductility means RC members have a stable deformation without a rapid and substantial reduction in the lateral strength of the RC members subjected to strong earthquake (e.g. after drift ratio of 1/50). Lateral stiffness is to evaluate the capacity of RC members resisting to their lateral deformation and to conduct an effective analysis of the global behaviour of RC structures. In addition, energy dissipation capacity reflects the ability of RC elements to absorb the earthquake energy caused by underground vibration, which usually dissipate the energy through the inelastic damage of the members or some additional damping devices. Referring to Fig.7, the detailed definition and description of the above indexes are summarized as below.

(1) Initial stiffness

The initial stiffness indexes discussed in this paper include initial elastic deformation stiffness $K_{int}$ and nominal initial stiffness $K_y$ (yielding stiffness) shown in Fig.7. As reported by Paulay and Priestley (1992), the quantity of the stiffness indexes related to lateral loads to ensure structural deformations. The two stiffness indexes are calculated secant displacement stiffness when the lateral displacements are 0.33 and 1.0 times the measured yielding displacement ($\Delta_y$) of the member, respectively. In this study, the yielding displacement $\Delta_y$ is a measured value of the lateral displacement obtained from the skeleton curve of load-displacement of the elements when an obvious inflection point (yielding point) of the skeleton curve occurs or when certain longitudinal reinforcement in the shear walls yields.

(2) Ductility indexes

Based on the previous studies, several methods to define the ductility of RC members have been proposed, including displacement and curvature ductility. For instance, energy method, 0.75 (Ghee et al. 1989) or 0.85-time ultimate lateral force, and equal-area method. In this study, referring to the research results reported by Ghee et al. (1989) and through measured yielding displacement ($\Delta_y$), maximum lateral displacement ($\Delta_{max}$) and ultimate displacement ($\Delta_u$) corresponding to $85\% V_{max}$
(Paulay and Priestley 1992; Pam et al. 2001; Memon and Sheikh 2005; Osorio et al. 2014), the maximum and ultimate ductility indexes are defined as,

\[ \mu_{\text{max}} = \frac{\Delta_{\text{max}}}{\Delta_y} \]  

(1)

\[ \mu_u = \frac{\Delta_u}{\Delta_y} \]  

(2)

(3) Inter-storey drift ratio

The ultimate inter-storey drift ratio \( \delta_u \) is one of the important parameters to evaluate the deformation capacity of RC elements and in relation to the height of the elements. It is expressed as,

\[ \delta_u = \frac{\Delta_u}{H} \]  

(3)

(4) Total dissipated energy

Energy dissipation is a fundamental structural property of RC elements when subjected to seismic demands. Energy dissipated of certain completed load cycle \( (i^{th} \) loop) \( (E_i) \) is calculated by the area of load-displacement curve encircled by this cycle, shown as the hatched area in Fig.7. The total dissipated energy of RC members is a sum of all cycles of the loading until the lateral force of the member reduce to 85%\( V_{\text{max}} \), is given by,

\[ E_T = \sum_{i=1}^{n} E_i \]  

(4)

(5) Total work index \( I_{wo} \)

To evaluate the serviceability of RC elements subjected to a given loading history, Gosain et al. (1977) propose a total work index \( I_{wo} \) which is expressed as,

\[ I_{wo} = \frac{1}{V_{\text{max}} \Delta_y} \sum_{i=1}^{n} V_{i,\text{max}} \Delta_{i,\text{max}} \]  

(5)

(6) Energy index \( I_E \)

Ehsani and Wight (1990) suggested a damage index \( I_E \) to evaluate the damage degree of RC elements subjected to a given load history which is given by
Table 2 gives a summary of the results of all above-mentioned indexes of the tested CSW specimens. It was found that the use of steel fibre improved the initial stiffness, ultimate ductility, and energy dissipation and working properties of the CSWs. This is attributed to two aspects, i.e. steel fibre restricts the crack propagation of concrete at the ends of shear walls at early stage and reduces the degradation of lateral resistance force at later stage. To be specific, the main benefits of steel fibre in RC CSW are,

(a) SFSWs have a higher initial stiffness of about 1.4 times the one of RC CSW for the bridging effect of the steel fibre in the concrete (Yap et al. 2016; Bharti et al. 2017);

(b) Steel fibre has a positive influence on the maximum lateral resistance capacity of RC CSWs which indicates the shear resistance of SFSWs is partly from the shear contribution of SFRC of coupling beams before they stop their coupling action;

(c) The maximum ductility levels ($\mu_{\text{max}}$) of the two SFRC CSWs are 1.06 and 1.38 times the one of RC CSW when the volume fractions of steel fibre in concrete are 1% and 2% respectively;

(d) When the used volume fraction of steel fibres is 1%, though steel fibre did not enhance the yielding displacement and inter-storey deformation capacity of the CSW, the ultimate ductility of this specimen is 1.05 times one of RC CSW and their energy dissipation capacity, energy index and total work index increased in 40%-60% comparing with the ones of the reference specimen.

(7) Lateral secant stiffness vs. displacement

It is significant to RC structures to understand the degradation of lateral stiffness of RC members under cyclic loads. Fig. 8 shows the development of the lateral secant stiffness of all tested CSWs with
their lateral displacement. Because steel fibre resists the cracking of concrete located at the ends of shear walls due to its bridging effect, the lateral secant stiffness of SFRC CSWs is higher than the one in normal concrete at early stage. However, the degradation degree of the lateral stiffness of all CSWs increases sharply before the lateral displacement of the members reaches their yielding displacement $\Delta_y$. Experimental observations verified that the deformation of the entire CSW was resisted by developing the flexural cracks at the ends of shear walls and the shear cracks on the shear walls at the second and third floor. At the later stage, the changing amplitude of the lateral stiffness of all specimens is quite gentle. This was explained by the facts that just a few new cracks were found in the CSWs at this stage and steel fibres stop their effective resistance to wide opened cracks.

4 Analysis and modelling of skeleton curve and hysteretic loop

5.1 Modelling of skeleton curve of SFSWs

In order to model the skeleton curve of the hysteretic behaviour of the RC members subjected to cyclic loads, the most widely-applied restoring force model is tri-linear restoring force model shown in Fig.9. The line 1 plotted in this figure presents three main feature points of the modelling curve of normal RC elements, i.e. cracking, yielding and maximum strength points respectively. For normal RC members, the yielding point could be quite different among different kinds of structural members due to the reduction of lateral stiffness after cracking. In well-designed SFRC elements, however, the lateral resistance of members after ultimate strength is still considerable and decreases slightly with the displacement as Line 2 shown in Fig.9. The experimental results of the study show the lateral stiffness of RC CSWs usually varies before they reach their maximum lateral force and the total degradation of the stiffness cannot be ignored. Therefore, a simplified tri-linear model based on FRC beam/columns model was suggested as Line 3 shown in Fig.9.

5.1.1 Definition of yielding point
Generally, it was considered that the yielding point of RC members is reached when certain longitudinal reinforcement yields or when the lateral force of the elements reaches 75-85% of their maximum (ideal calculated or measured) strength (e.g. Ghee et al. 1989; Bayrak and Sheikh 1997). However, in CSW systems, although SFRC coupling beam can provide a good coupling effect for its high performance, the integrity of the systems is weak and significantly affects the lateral stiffness of the entire member. This then influences the yielding of the CSW members. Referring to the research, it is suggested that the lateral force of CSWs usually reaches 65% of their maximum strength when the members yield in this study. Therefore, the yielding strength of SFSWs is calculated as,

\[ F_y = \alpha_y F_u = 0.65 F_u \]  \hspace{1cm} (7)

\[ K_y = \beta_y K_{int} \]  \hspace{1cm} (8)

As described previously, the lateral stiffness of SFSWs has no very obvious changes before cracking of the members, which is considered as a reduced initial stiffness \( K_{int} \). Therefore, the yielding stiffness of SFRW is expressed as Eq. (8). Regarding the reduction ratio of the initial stiffness of single SFRC shear wall at the yielding situation, Zhao and Dun (2014) reported that it could be taken as 0.29 for predicting the yielding stiffness. In this paper, \( K_{int} \) is calculated on the basic of the Chinese standard JGJ3-2010 (CIS 2010) and given by,

\[ K_{int} = \frac{3E_s I_{eq}}{H^3} = \frac{1}{H^3} \left( \frac{3E_s I_w}{1 + \frac{9 \mu \nu}{A_w H^2}} \right) \]  \hspace{1cm} (9)

In SFRC CSWs, however, SFRC coupling beams improve the whole behaviour of the member which then affects the development of lateral stiffness at this stage. Then, this positive effect of steel fibre decreases greatly if the capacity of RC coupling beam is higher than the one of shear walls. This is attributed to that the moment distribution and corresponding deformations of the various parts of CSWs significantly are dependent on their stiffness level. The results of the present research already verified the above analysis and present that the values of the reduction ratios of SFSW1-3 are 0.14,
0.19 and 0.16, respectively. Therefore, the change of lateral stiffness of SFSWs is affected by three parts, i.e. the nonlinear behaviour of steel rebar and SFRC, and the reduction in the confinement of coupling beams. With the above considerations, when the volume fraction of steel fibre in SFSWs ranges from 1% to 2%, the simplified stiffness reduction ratio $\beta$ is suggested to take as 0.2.

5.1.2 Definition of maximum strength point—$M_{max}$ and $K_{max}$

As described previously, a well-design RC CSW system works similarly to a single RC shear wall before reaching their maximum resistance status. Therefore, RC CSW is considered as an I-type RC elements with openings same as reported by Zhao and Dun (2014). The design also should consider the coupling effect of coupling beam and the resistance of the shear walls. Considering the positive effect of RC edge columns and steel fibre on the entire behaviour of CSWs, a simplified calculation model to predict the moment capacity of SFSWs $M_{max}$ consisting of the moment resistance compositions from transverse reinforcement ($M_s$), longitudinal steel of RC edge columns ($M_{sl}$), enhancement effect of axial load ($M_a$) and SFRC ($M_{FRC}$) and is expressed as,

$$M_{max} = M_s + M_{sl} + M_a + M_{FRC}$$

In this equation, based on a detailed sectional analysis of RC/SFRC CSWs, the compositions provided by the parts of the CSWs are summarized in Eqs. (11) to (14).

$$M_s = \frac{A_w fyw}{2h_{wo}} (h_u - h_b - 1.5x)(h_u - h_b + 0.5x)$$

(11)

$$M_{sl} = f_y A_s (h_u - h_b)$$

(12)

$$M_a = \frac{1}{2} N(h_{wo} - h_b)$$

(13)

$$M_{FRC} = f_{\beta F} b \times (h_u - \frac{x_i}{2} - \frac{x}{2})$$

(14)

where, the concrete compressive strength of SFRC is calculated by the model proposed by Zhang (2007) and detailed information is reached in the research reported by Zhao and Dun (2014). Through the maximum moment of RC CSWs, the maximum lateral resistance force $F_{\text{max}}$ is obtained.
On the other hand, with the considerations of the entire resistance of CSWs is less than a single shear wall with the same conditions (cross-section, reinforcements and concrete etc.), a reduction factor is introduced to modify the maximum moment $M_{\text{max}}$ of the CSWs based on the original calculation of the two signal shear walls. To simplify the calculation procedure, the reduction factor is suggested as 0.95 for the reference RC CSWs. Due to steel fibres improved the entire lateral resistance of RC CSW system, the reduction factor is taken as 0.9 for the SFRC CSWs in this study. About the lateral stiffness from yielding point to maximum strength point ($K_{\text{max}}$), as presented previously, the lateral stiffness $K_{\text{max}}$ of CSWs is assumed as 0.3 times initial stiffness, $0.3K_{\text{int}}$, referring to the experimental results in this study.

5.1.3 Definition of post-peak point of skeleton curve — $F_u$ and $K_u$

Ultimate strength $F_u$ — A number of researchers suggested the ultimate strength of RC elements (e.g. columns) was taken as 80%-90% of their maximum strength (Bayrak and Sheikh 1997). In this study, the ultimate strengths of SFRC CSWs were considered as 85% of the maximum strength, i.e. $0.85F_{\text{max}}$ (Hwang et al. 2005; Zhao and Dun 2014).

Lateral stiffness at post-peak $K_u$ — Due to the post-peak behaviour of RC CSWs is improved by steel fibre, the reduction of lateral stiffnesses of SFCSWs should be slower than the one in normal CSW at this stage. Additionally, owing to coupling beams stop providing lateral resistance at the large deformation stage, the main influence factors of the stiffness are fibre concrete compressive strength and the volume fraction of steel fibre. In this paper, the lateral stiffness at post-peak was calculated as an equivalent stiffness multiplying an affecting ratio $\beta_{su}$ to the initial stiffness $K_{\text{int}}$. In each individual shear wall in CSW system, Zhao and Dun (2014) indicated the affecting ratio could be near to -0.02 for SFRC shear walls. Therefore, with the consideration of the weak structural integrity of the CSW system but the good coupling action of SFRC coupling beams in SFSWs, $\beta_{su}$ is taken as 60~70% of the one of sign SFRC shear wall, i.e. $K_u$ is -0.013 times of the initial stiffness $K_{\text{int}}$. 

20
5.1.4 Complete skeleton model

Based on the above analyses, the complete skeleton model curve of SFSWs (the volume fraction of steel fibre: 1%-2%) is expressed as,

\[
F = \begin{cases} 
K_y \Delta_x = \beta_y K_{int} \Delta_x & 0 \leq \Delta_x \leq \Delta_y \\
K_y \Delta_x + 0.03 K_{int} (\Delta_x - \Delta_y) & -\Delta_{max} \leq \Delta_x \leq -\Delta_y \text{ and } \Delta_y \leq \Delta_x \leq \Delta_{max} \\
K_y \Delta_x - 0.013 K_{int} (\Delta_x - \Delta_y) & -\Delta_{u} \leq \Delta_x \leq -\Delta_{max} \text{ and } \Delta_{max} \leq \Delta_x \leq \Delta_{u}
\end{cases}
\] (15)

5.1.5 Experimental verification of proposed model

To check the proposed model curve, some new research results (Meng 2013) were used. As shown in Fig.10, the calculated skeleton curves present a good agreement with the experimental curves which illustrate the proposed model can be used to predict the skeleton curve of the load-displacement of the SFSWs subjected to seismic loads.

5.2 Modelling of hysteretic curve of RC/FRC CSWs

5.2.1 Calibration of the rule for hysteretic curve

(a) Before yielding of CSW members

Taking specimen SFSW-1 as an example shown in Fig.11 (a), according to the experimental results of the current study, the non-elastic deformation of CSW is slight before it reaches its yielding status. It means the plastic dissipated energy of the member could be ignored. Therefore, in this paper, the rule of the hysteretic curve before the yielding of the member is simply considered as a linear uploading or unloading cycle.

(b) From yielding point to maximum strength point

Before CSW reaches its maximum strength or coupling beams stop providing deformation resistance, the restoring force rules of SFSW are same or similar as the ones of signal coupling beam/shear wall. Therefore, referring to the research results reported by Zhao and Dun (2014) and the experimental result in the current study shown in Fig.11 (b), a simplified restoring force model of SFSW are
obtained shown in Fig.12, including some key feature points (Points 1-8). The definition of the points is concluded as the following sections.

1) Fixed feature points 1 and 5

As shown in Fig.12, each of hysteretic loops of the load-displacement curve has two key fixed points on its uploading and unloading branch, respectively. The lateral forces corresponding to the two points both are 0.3 times of yielding strength at the both directions. Due to the hysteretic behaviour is elastic, therefore, the two point was defined as \((0.3\Delta_y, 0.3F_y)\) and \((-0.3\Delta_y, -0.3F_y)\), respectively.

2) Stiffness inflection points 2 and 6

Based on the investigation results in this study and reported by Zhao and Dun (2014), the inflection points of lateral stiffness of each of loops occur when the lateral displacement of the member reaches its corresponding yielding displacement level shown in Fig.12.

3) End points 4 and 8 of initial unloading, \(F_{4,8}\)

The initial unloading actions of SFSWs are stable (Lines 3-4 and 7-8) in the CSWs and will finish at a stable lateral force, as shown the lateral force at the points 4 and 8 in Fig.12. In this study, this stable lateral force is taken as 0.2 times yielding strength \(F_y\).

5.2.3 Rules of hysteretic curve after maximum strength

Though the failure mode of all specimens is flexural-dominant failure, the skeleton curves of the CSW members after maximum strength is shorter than the one of individual shear walls or coupling beams. Therefore, the rules of the hysteretic curve after maximum strength are considered as same as that from yielding point to maximum strength point.

5.2.4 Stiffness of hysteretic model \(K_{23}\) and \(K_{67}\)

Before the yielding of SFSW members, the stiffness of uploading is simplified as \(K_y\). Based on the study, the various stiffnesses at post-yielding, i.e. the slop from yielding point to ultimate point, are obtained and shown in Fig.12.

5.3 Verification of the proposed hysteretic model
In order to confirm the proposed complete hysteretic model proposed, several representative loops of each specimen were used from the present study and the previous results (Meng 2013). These representative loops include the ones near to the cracking status, yielding status, maximum strength or ultimate strength status. Fig.13 shows the comparison results between experimental and predicated hysteretic loops which indicts that the proposed complete model assesses the hysteretic cycles of the RC/SFRC CSWs with a good agreement.

6 Conclusions

This paper experimentally investigated the hysteretic behaviour of SFRC CSWs under simulated seismic loads. The strength, deformation and stiffness degradation, energy dissipation and crack damage of the elements have been discussed. Main conclusions were drawn as follows.

(1) Steel fibres improve the stress distribution of RC CSWs in terms of lateral resistance capacity stiffness, and deformation. This is attributed to the fact that steel fibres improve the non-uniform situation of the stress of shear walls which makes the reinforcements provide more effective tensile resistance in the walls. Therefore, the deformation of entire CSW was realized by developing the flexural cracks at the ends of the shear walls and the shear-type cracks at the shear walls of the upper floors.

(2) Comparing with RC CSW specimens, SFRC CSWs presented a plump hysteretic behaviour with a higher lateral stiffness and strength, and more stable degradation of lateral resistance post-peak. Steel fibres delay the crack propagation of RC CSW specimens and the concrete crushing at the joint zone.

(3) Steel fibres improve the integrity of RC CSWs and the degradation of lateral stiffness of the members due to the tensile resistance of reinforcements in coupling beams is effectively used. This is because steel fibres improve the energy dissipation and deformation of coupling beam which was verified by the observed results of the reinforcement fracture in RC edge columns.
(4) Considering the coupling effectiveness of coupling beams, using a simplified strength model based on the sectional analysis of an individual shear wall, a maximum strength model has been developed for SFRC CSW specimens. Using the strength model, a simplified skeleton curve model and a hysteretic model were proposed for RC/SFRC CSWs. Results verified the proposed models can predict the experimental results and existing data with a good agreement.

Acknowledgement

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Notations

\[ E_{ic} \] — equivalent stiffness, where \( E_c \) is elasticity modulus of concrete;

\[ I_w \] — moment of inertia of the entire cross-section of shear wall;

\[ A_w \] — area of cross section of wall without openings reported by CIS (2002);

\[ \mu \] — calculation factor of the shape of cross-section taken as 1.2 for the rectangular section;

\[ A_{sw}, A_s \] — cross area of longitudinal steel rebars in the shear wall and edge columns;

\[ f_{yw}, f_y \] — yielding strength of longitudinal steel in the shear wall and edge columns;

\[ x, h_w, h_{wo}, b_w, h_b, H \] — calculation height of compressive zone and tensile zone which is taken as \( x = h_w - 1.25 x \);

\[ h_{wo}, \mu_v \] — height and effective height of cross section respectively;

\[ b_w, h_b, H \] — the width of the cross-section, and height of columns and a total height of shear walls

\[ f_{fb} \] — bending tensile strength of FRC, which can be calculated as \( 0.4f_{fts} \);

\[ f_{c}, f_{fts} \] — compression strength, splitting tensile strength of FRC obtained from test or the model proposed by Han et al. (2006);

\[ \Delta_x, \Delta_y \] — yielding displacement ultimate displacement of the member when 85% \( V_{max} \);

\[ \delta_1, \mu_{max}, \mu_v \] — ultimate inter-storey drift ratio, the maximal and ultimate ductility of members;

\[ V_{max}, V_{max} \] — the maximum strength of member and the one at \( i \)th cycle;

\[ \Delta_{max}, \Delta_{max} \] — lateral displacement corresponding to \( V_{max} \) and \( V_{max} \), and the given \( x \) displacement;

\[ E, E, E \] — total, \( i \)th cycle and normalized dissipated energy of RC member;

\[ K_{min}, K_{max}, K_{a} \] — total work and energy indexes, and equivalent viscous damping coefficient of the member;

\[ \alpha, \beta \] — influencing factors for yielding strength and reduced stiffness;

\[ F_{y}, F_{max}, F_{i} \] — forces corresponding to yielding, maximum and ultimate displacements in envelop curve model; as well as the forces at \( i \) feature points of the skeleton curve model (\( i = 1-8 \));

\[ M_{a, max} \] — maximum moment capacity of member, and the moment provided by transverse steel;

\[ M_{iy}, M_{i, o}, M_{FRC} \] — the moment provided by longitudinal steel, axial load action, and fibre reinforced concrete;

References


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Fig. 7 Main assessment factors of RC members under seismic loads

The dissipated energy at ith cycle:

\[ E_i = \text{Area of Zone ABDF} \]

i th cycle

Note: All parameters are mean values calculated from both directions.
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Fig. 12 Proposed hysteretic model of RC/SFRC CSWs

\[
k_{23} = \frac{F_3 - F_2}{\Delta_3 - \Delta_2}, \quad k_{34} = K_y
\]

\[
k_{45} = \frac{F_5 - F_4}{\Delta_5 - \Delta_4} = \frac{0.2F_y - F_4}{\Delta_5 - \Delta_4}
\]

\[
k_{78} = K_y, \quad k_{81} = \frac{F_1 - F_8}{\Delta_1 - \Delta_8}
\]
Fig. 13 Comparison between experimental and predicted hysteretic cycles
Table 1 Details of main parameters of specimens

<table>
<thead>
<tr>
<th>Specimen No.</th>
<th>Coupling beam Length/width/height (mm)</th>
<th>SFRC</th>
<th>Steel fibre</th>
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</thead>
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<tr>
<td></td>
<td>f&lt;sub&gt;kc&lt;/sub&gt; (MPa)</td>
<td>f&lt;sub&gt;fts&lt;/sub&gt; (MPa)</td>
<td>Volume fraction</td>
</tr>
<tr>
<td>SFWS-1</td>
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<td>-</td>
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<tr>
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</tr>
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<td>SFWS-3</td>
<td>50.3</td>
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</tr>
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</table>

SFRC: Steel fibre reinforced concrete; f<sub>kc</sub>: SFRC compressive strength; f<sub>fts</sub>: Splitting tensile strength.

Table 2 Summary for the test results of CSWs in this study

<table>
<thead>
<tr>
<th>Specimens</th>
<th>V&lt;sub&gt;max&lt;/sub&gt; (kN)</th>
<th>K&lt;sub&gt;rot&lt;/sub&gt; (kN/mm)</th>
<th>K&lt;sub&gt;r&lt;/sub&gt; (kN/mm)</th>
<th>Δ&lt;sub&gt;r&lt;/sub&gt; (mm)</th>
<th>μ&lt;sub&gt;max&lt;/sub&gt;</th>
<th>μ&lt;sub&gt;μ&lt;/sub&gt;</th>
<th>δ&lt;sub&gt;μ&lt;/sub&gt;(%)</th>
<th>E&lt;sub&gt;r&lt;/sub&gt;(kN/mm)</th>
<th>E&lt;sub&gt;N&lt;/sub&gt;</th>
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<tr>
<td>SFWS-1</td>
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