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The correlation structure of longitudinal measurements of vision in patients with macular degeneration.

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RESEARCH ARTICLE

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Received 8 October 2009 Revised 5 January 2010, Accepted 11 January 2010 Published online in Wiley Interscience (www.interscience.wilev.com) DOI: 10.1002/pst.419 The correlation structure of longitudinal measurements of vision in patients with macular degeneration Tomasz Burzykowski^{a,b*} and M. Buyse^{a,b} Background: In age-related macular degeneration (ARMD) trials, the FDA-approved endpoint is the loss (or gain) of at least three lines of vision as compared to baseline. The use of such a response endpoint entails a potentially severe loss of information. A more efficient strategy could be obtained by using longitudinal measures of the change in visual acuity. In this paper we investigate, by using data from two randomized clinical trials, the mean and variance-covariance structures of the longitudinal measurements of the change in visual acuity. *Methods*: Individual patient data were collected in 234 patients in a randomized trial comparing interferon- α with placebo and in 1181 patients in a randomized trial comparing three active doses of pegaptanib with sham. A linear model for longitudinal data was used to analyze the repeated measurements of the change in visual acuity. Results: For both trials, the data were adequately summarized by a model that assumed a quadratic trend for the mean change in visual acuity over time, a power variance function, and an antedependence correlation structure. The power variance function was remarkably similar for the two datasets and involved the square root of the measurement time. Conclusions: The similarity of the estimated variance functions and correlation structures for both datasets indicates that these aspects may be a genuine feature of the measurements of changes in visual acuity in patients with ARMD. The feature can be used in the planning and analysis of trials that use visual acuity as the clinical endpoint of interest. Copyright 🔘 2010 John Wiley & Sons, Ltd. Keywords: visual acuity; longitudinal data; variance function; correlation structure

BACKGROUND

In age-related macular degeneration (ARMD) trials, the FDA approved endpoint is a binary response defined as the loss (or gain) of at least three lines of vision as compared to baseline one
 year after starting therapy. Secondary endpoints in ARMD trials include further binary responses defined as the loss (or gain) of
 more than a pre-defined number of lines of vision as compared to baseline at different time points.

The use of such response endpoints entails a potentially severe loss of information, for two main reasons. First, it does not allow to differentiate between patients who lose different numbers of lines of vision. Second, it does not take into account the information available at other time points. Additional problems of binary endpoints at fixed time points include misclassification of the outcome, potential for a ceiling or floor effect, and the need to impute missing data [1].

A more efficient strategy could be obtained by using longitudinal measures of the change in visual acuity, defined as the change in the number of letters correctly read as compared to baseline. It is worth noting that the binary response is actually closely linked to the change in visual acuity, because each line on the vision chart consists of five letters.
Thus, the number of incorrectly read letters gives approximate

information about the number of lines lost.
 An important difficulty in using longitudinal measurements of

An important difficulty in using longitudinal measurements of the change in visual acuity is the need to use models that correctly reflect the variability and dependence between the measurements. In this paper we show, by using data from several randomized clinical trials, that the mean and variance– covariance structures of the longitudinal measurements of the change in visual acuity can be described by relatively simple models that seem to fit the data well for two different experimental drugs. Use of these models should facilitate the planning and analysis of trials that use such measurements.

MATERIAL AND METHODS

Trials

The first of the two randomized trials included in our analyses compared interferon- α with placebo [2]. The second trial compared different three doses (0.3, 1, and 3 mg) of intravitreous injections of pegaptanib, an anti-vascular endothelial growth factor therapy, or sham injections (with a syringe applied on the surface of the eye to simulate the pressure of

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an injection), every 6 weeks over a period of one year [3]. Tables I and II present summary characteristics of the measurements of the change in visual acuity versus baseline obtained in the two trials.

Methods

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7 The longitudinal measurements of the change in visual acuity versus baseline were analyzed by using a general linear model a for longitudinal data [4]. For each treatment arm, the mean value of the change in visual acuity was modelled as a quadratic 11 function of time, with treatment-specific coefficients. Three forms of the variance-covariance structure of the visual acuity 13 measurements were assumed. Model 1 used a general structure with unconstrained correlations and variances. Model 2 speci-15 fied an antedependence correlation structure, with unconstrained variances. Model 3 assumed an antedependence 17 correlation structure and variances expressed as a power function of time. Finally, Model 4 was similar to Model 3, but 19 the correlation coefficients, which defined the antedependence structure, were modeled as a linear function of time on the scale 21 defined by Fisher's Z-transform.

The general variance–covariance structure assumes that variances of the longitudinal measurements of change in visual acuity differ freely between time points. Thus, for subsequent *K* measurements, different *K* variances are assumed. Additionally, the correlation matrix for the measurements is expressed as follows:

	(1	$\rho_{1,2}$		$\rho_{1,K-1}$	$\rho_{1,K}$
29	ρ _{1,2}	1		$\rho_{\rm 2, K-1}$	$ ho_{\mathrm{2,K}}$
31	:	÷	·	÷	:
51	$ ho_{1,K-1}$	$ ho_{2,K-1}$		1	$\rho_{K-1,K}$
33	$\langle \rho_{1,K}$	$ ho_{2,K}$		$\rho_{K-1,K}$	- I /

Thus, it is defined by the values of K(K+1)/2 correlation coefficients $\rho_{1,2}, \rho_{1,3}, \ldots, \rho_{K-1,K}$, where ρ_{ij} is the correlation coefficient between the *i*th and the *j*th measurement. (We assume that, within a trial, the measurements were made for all patients at approximately the same sequence of time points.) It follows that Model 1 described the variance–covariance structure by using K(K+1)/2+K = K(K+3)/2 parameters.

The antedependence correlation structure [5] is defined as follows:

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Table I.	Summary statistics for the change in visual acuity	
measurer	nents obtained in the interferon- α trial.	

Interferon-α			Placebo			
Week	Ν	Mean (SD)	Ν	Mean (SD)		
4	114	-3.51 (8.86)	117	-1.30 (7.71)		
12	110	-5.88 (11.62)	117	-2.27 (11.73)		
24	102	-9.07 (14.08)	112	-5.70 (13.83)		
52	90	—15.48 (15.28)	105	-11.18 (16.42)		
N = num	ber of r	neasurements; SD =	standar	d deviation.		

Additionally, the correlation coefficients, which defined the antedependence structure, were assumed to depend linearly on time on the scale defined by Fisher's *Z*-transformation. More specifically, the model assumed that

$$z_i = \log(1+\rho_i) - \log(1-\rho_i) = \gamma_0 + \gamma_1 t_i$$

where ρ_i is the *i*th of the *K*-1 correlation coefficients, which define the antedependence structure, and t_i is the first time coordinate of the coefficient (recall that ρ_i is the correlation coefficient between the *i*th and the (*i*+1)th measurement). 23 Consequently, the model described the variance-covariance structure by using only 2+2=4 parameters. Thus, it was the most parsimonious one among the four considered models.

It is worth noting that Models 1–4 define a sequence of nested models, with Model 4 nested within Model 3, Model 3 nested within Model 2, and Model 2 nested within Model 1.

The fit of each of the four models was assessed by using the scaled residuals [6]. The residuals should be approximately uncorrelated and follow the standard normal distribution. The normality assumption was checked by using the normal *Q-Q* 33 plot. Between the models, the fit was compared by using the restricted-likelihood-ratio test (LRT) and the Akaike Information 35 Criterion (AIC) [4]. The latter was based on the number of variance–covariance parameters, given that all compared 37 models had the same mean structure.

The calculations were performed using SAS v.9.3 PROC MIXED (Models 1 and 2) and self-written SAS-IML code (Models 3 and 4).



Thus, it is defined by the values of only K-1 coefficients, $\rho_1, \rho_2, \ldots, \rho_{K-1}$, where ρ_i is the correlation coefficient between the *i*th and the (*i*+1)th measurement. It follows that Model 2 described the variance-covariance structure by using K-1+K=2K-1 parameters.

Model 3 assumed the antedependence correlation structure. Additionally, it assumed that the variance of the measurements of change in visual acuity at time *t* was equal to $\sigma^2 t^{\delta}$. Thus, it used only two parameters, σ and δ , to express the different *K* variances. Consequently, it described the variance–covariance structure by using only *K*–1+2=*K*+1 parameters.

Finally, Model 4 assumed both the antedependence correlation structure and the power-of-time variance function.

RESULTS

The interferon- α trial

Table III shows the values of minus twice log-restricted-likelihood, the number of variance-covariance parameters, and57the resulting values of the AIC for Models 1–4. For none of the59Models 2–4, the difference in minus twice log-restricted-59likelihood with respect to Model 1 is statistically significant at61models offers a fit comparable to (the most general) Model 1.61

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		0.3 mg		1 mg		3 mg		Sham	
Week	Ν	Mean (SD)	Ν	Mean (SD)	Ν	Mean (SD)	Ν	Mean (SD)	
б	286	-1.56 (9.20)	292	-1.23 (9.82)	286	-2.37 (10.13)	291	-4.08 (9.66)	
12	289	-3.14 (11.56)	291	-2.17 (11.21)	283	-4.20 (12.19)	288	-6.36 (11.32)	
18	269	-3.69 (12.12)	291	-3.91 (12.15)	281	-5.42 (13.82)	287	-8.72 (12.56)	
24	273	-4.06 (13.21)	287	-4.29 (13.33)	283	-6.23 (14.30)	281	-9.85 (13.98)	
30	271	-4.94 (14.20)	285	-5.01 (13.90)	278	-7.20 (15.47)	282	-11.59 (15.95)	
36	265	-5.84 (14.51)	278	-5.28 (14.79)	273	-7.28 (15.22)	278	-12.42 (15.89)	
12	271	-6.49 (14.82)	270	-6.09 (15.14)	267	-7.62 (16.19)	275	—13.16 (16.16)	
18	266	-6.83 (15.18)	267	-5.85 (15.37)	259	-8.35 (16.59)	269	-13.48 (16.84)	
54	271	-7.55 (15.65)	275	-6.75 (16.11)	264	-10.30 (16.66)	275	-14.78 (17.73)	
V = numł	per of me	asurements; SD = sta	andard dev	viation.					
Table II Models	I. Minus 1–4.	twice log-restricted-	likelihood	(–2REML), number	of variance	e-covariance paramet	ers, and th	ne resulting AIC for	
		Inter	feron-α tri	al		Pegap	tanib trial		
			of noromo						

	-2REML	No. of parameters	AIC	-2REML	No. of parameters	AIC		
Model 1	6400.1	10	6420.1	68 067.4	45	68 157.4		
Model 2	6405.6	7	6419.6	68 366.3	17	68 400.3		
Model 3	6407.0	5	6417.0	68 379.4	10	68 399.4		
Model 4	6407.4	4	6415.4	68 415.6	4	68 423.6		



Figure 1. Normal Q-Q plots for the scaled residuals for Model 3 fitted to the interferon- α trial data.

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Figure 2. Observed and predicted mean values of the change in visual acuity for the interferon- α trial, using Model 3.

The observed AIC values indicate that all four models present a similar fit to the data. Formally speaking, the lowest AIC value (6417.0), indicating the best fit, is obtained for Model 4. However, the AIC value (6415.4) for Model 3 is not much different.

Figure 1 shows the normal Q-Q plots for the scaled residuals at each measurement time point for Model 3. The plots suggest a satisfactory fit of the model. This conclusion is confirmed by Figure 2, which presents the observed and predicted means of the visual acuity change for the two treatment arms of the interferon- α trial. The plot indicates a linear mean trend for both arms. This is confirmed by the 95% confidence intervals of the estimated coefficients, which are shown in Table IV. The intervals for the time-squared coefficient include 0, suggesting that a linear function of time is adequate to describe the mean trend.

According to Model 3, the variance of the change in visual acuity at time t is approximately equal to $(5.7)^2 t^{1/2} =$ $32.5\sqrt{t}$. The 4 × 4 correlation matrix of the four visual acuity

	Interferon-a trial		Pegaptanib trial				
	Interferon-a	Placebo	0.3 mg	1 mg	3 mg	Sham	
Intercept	-2.28	-0.33	-1.22	-0.82	-0.03	-1.66	
	(-4.14,-0.42)	(-2.17,1.50)	(-2.63,0.18)	(-2.22,0.59)	(-1.43,1.37)	(-3.06,-0.26)	
Time	-0.30	-0.23	-0.21	-0.19	-0.21	-0.42	
	(-0.50,-0.10)	(-0.43,-0.04)	(-0.33,-0.10)	(-0.31,-0.07)	(-0.33,-0.09)	(-0.54, -0.31)	
Time ²	0.0006	0.0005	0.0009	0.001	0.001	0.003	
	(-0.002,0.004)	(-0.002,0.004)	(-0.001,0.003)	(-0.001,0.003)	(-0.0004,0.003)	(0.001,0.005)	

	Interfe	eron- α trial	Pegap	Pegaptanib trial		
Parameter	Model 3	Model 4*	Model 3	Model 4*		
σ	5.73	5.73	6.27	6.57		
	(4.96,6.63)	(4.95,6.62)	(5.79,6.78)	(6.07,7.10)		
δ	0.28	0.28	0.25	0.23		
	(0.22,0.33)	(0.23,0.33)	(0.22,0.27)	(0.21,0.26)		
<i>0</i> ₁	0.60	0.58	0.73	0.77		
	(0.51,0.67)	(0.50,0.66)	(0.70,0.75)	(0.75,0.79)		
07	0.66	0.67	0.81	0.81		
-	(0.58,0.72)	(0.62,0.72)	(0.79,0.83)	(0.79,0.82)		
03	0.78	0.77	0.85	0.84		
5	(0.72,0.83)	(0.71,0.82)	(0.84,0.87)	(0.82,0.84)		
04			0.88	0.86		
			(0.86,0.89)	(0.85,0.87)		
05	_	_	0.88	0.88		
5			(0.87,0.89)	(0.87,0.89)		
06	_	_	0.91	0.90		
0			(0.90,0.92)	(0.89,0.91)		
07		_	0.92	0.92		
			(0.91,0.93)	(0.91,0.92)		
0 ₈		_	0.93	0.93		
0			(0.92,0.93)	(0.92, 0.94)		
² 0	_	1.19		1.87		
~		(0.91 1.48)		(177 196)		

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change measurements can be expressed by using only three correlation coefficients ρ_1 , ρ_2 , and ρ_3 . The estimated values of the coefficients are displayed in Table V. The table also contains the estimates obtained for Model 4.

The panel on the left-hand side of Figure 3 presents the sample variances and the corresponding model-based estimates for Model 3. Apart from a slight overestimation at 52 weeks, the model-based estimates are in a very good agreement with the sample variances.

Similarly, the panel on the left-hand side of Figure 4 presents the sample correlations and their corresponding model-based

estimates for Model 3. Again, a very close agreement between the two sets of estimates can be observed.

The pegaptanib trial

The values of minus twice log-restricted-likelihood, the number of variance–covariance parameters, and the resulting values of the AIC for Models 1–4 are shown in Table III. The difference in minus twice log-restricted-likelihood between Models 1 and 2 is statistically significant at the 0.05 significance level. Also, the lowest AIC value, indicating the best fit, is obtained for Model 1. 51

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Figure 6. Observed and predicted mean values of the change in visual acuity for the pegaptanib trial, using Model 3.

Given that the data included up to nine visual acuity change measurements for a single patient, this result might be expected, because the variance-covariance structure of the measurements might be potentially complex. However, it is so worth noting that, according to the AIC values, Model 3 offers a better fit than both the simpler Model 4 and the more complex Model 2. Also, the result of the LRT comparing Models 2 and 3 is not statistically significant at the 0.05 significance level. Moreover, the fit of Model 3 is quite satisfactory, as can be seen from the normal *Q-Q* plots for the

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scaled residuals at each measurement time point (Figure 5) and
from the plot of the observed and predicted means of the visual acuity change for the four treatment arms (Figure 6). As Model 3
is more parsimonious, it is preferred over Model 1. The plot and the 95% confidence intervals of the estimated coefficients, which are shown in Table IV, suggest a quadratic mean trend for the sham group and linear trends for the active treatment
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According to Model 3, the variance of the change in visual acuity at time *t* is approximately equal to $(6.3)^2 t^{1/2} = 39.7 \sqrt{t}$. The 9 × 9 correlation matrix of the four visual acuity change measurements can be expressed by using only eight correlation coefficients $\rho_1, \rho_2, \ldots, \rho_8$. The estimated values of the coefficients are displayed in Table IV.

The panel on the right-hand side of Figure 3 presents the 47 sample variances and the corresponding model-based estimates for Model 3. Apart from a slight underestimation at 30 weeks, 49 the model-based estimates are in an excellent good agreement 51 with the sample variances. The panel on the right-hand side of Figure 4 presents the sample correlations and their corresponding model-based estimates for Model 3. For correlations below 53 0.7, i.e. for visual acuity measurements made at more separated 55 time points, the model-based estimates are lower than their sample-based counterparts. Note, however, that the latter do not 57 take into account the differences due to the treatment effects.

Both trials

Figure 7 presents Fisher's Z-transformation of the estimates of the 61 antedependence structure defining the correlation coefficients for



Figure 7. Fisher's Z-transformation of the estimated correlation coefficients defining the correlation structure of Model 3. The straight lines are obtained from Model 4 and describe the linear dependence of the transformed coefficients on their first time coordinates (indicated on the horizontal axis).

23 both trials (Table V). The plot includes the straight lines obtained from Model 4 that describe the linear dependence of the 25 transformed coefficients on their first time coordinates. The plot illustrates that the Z-transformation of the correlation coefficients 27 increases linearly in time, with approximately the same slope for the two trials, but with a different intercept. The linear equations 29 are z = 1.195 (SE 0.145)+0.036 (SE 0.009) $\cdot t$ for the interferon- α trial and z = 1.869 (SE 0.049)+0.030 (SE 0.002) $\cdot t$ for the pegaptanib 31 trial. Thus, the difference in slopes does not differ statistically from 0 (95% confidence interval, CI (-0.012, 0.024)), whereas the 33 vertical shift between the lines in Figure 7 is approximately

constant and equal to 0.674 (95% CI (0.368, 0.980)). 35

DISCUSSION

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The analysis reveals remarkably consistent results regarding the variance-covariance structure of the longitudinal measurements 39 of the change in visual acuity versus baseline. First, the variance of the measurements can be approximately expressed as a 41 constant (close to 36) times the square root of the time at which the measurement was taken. Second, the correlations of the 43 measurements can be expressed by using the antedependence structure. Moreover, the correlation coefficients, defining the 45 antedependence structure, are linearly increasing with time with the same slope, but with different intercepts (on Fisher's 47 Z-transformation scale).

These results can be used in designing experiments, in which the use of longitudinal measurements of the change in visual acuity versus baseline is of interest. In particular, they can be used for sample size calculations [4,7].

It would be of interest to validate our results by using data from randomized trials with other drugs recently approved for ARMD. Interferon- α was shown not to have any significant impact on the visual acuity of patients with ARMD [1]; hence, the correlation structure identified in the interferon- α trial may well reflect the natural history of the disease and the intrinsic variability of visual acuity measurements. On the contrary, 11 pegaptanib had a highly significant effect on visual acuity, but it did not seem to affect the correlation structure of repeated 13 measurements of visual acuity to any great extent. It is tempting, therefore, to hypothesize that treatments for ARMD 15 affect the mean values of the measurements' visual acuity over time, but not their correlation structure. This hypothesis awaits 17 further confirmation.

Acknowledgement

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