

# Measuring Driver's Relative Performance Over Time Using DEA and Window Analysis



# Co-authors

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# Introduction

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- ❑ Among different road user types, drivers represent the largest share of road fatalities. As a result, more attention should be paid to the behavior of drivers.
- ❑ Driving performance of a driver should be evaluated not only at a specific point of time but also over a time period.
- ❑ Horizontal curves, particularly on two-lane rural roads, have been recognized as a significant safety issue for many years

# Data collection on a curve taking scenario

**Driving simulator** Fixed-base STISIM, M400 with 180°parabollic screen



Width of 2.8m & posted speed limit of 70 km/h

## Participants

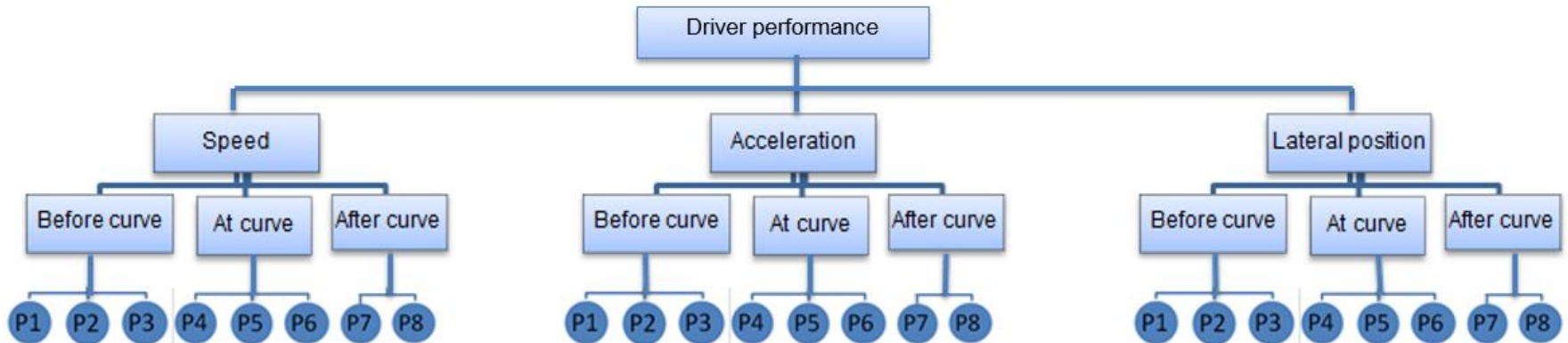
- 20 Volunteers
- 6 Excluded: 2 simulator sickness, 4 missing data
- 14 Participants in dataset; 8 men Age: 18-54; mean age 26.32; SD 10.47

# Data collection on a curve taking scenario- cont.

All participants completed five same trips of 16.2 km for five different days

## Indicators

- **Speed** The resultant of longitudinal and lateral speed is used
- **Acceleration** The resultant of longitudinal and lateral acceleration is used
- **Lateral position** The distance between the center of the road and the vehicle's longitudinal axis



# Model Preparation

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Before analysing, the raw data needed to be processed for each point separately.

- In each of the eight points, **ordinal grades** were assigned for **speed, acceleration and lateral position** illustrating the degree of each driver's performance on that parameter at that particular measurement point.
- The higher the grade, the better the performance.
- Moreover, weight restrictions were added in order to guarantee the consistency with prior knowledge and the obtainment of acceptable layer-specific weights

# Time window analysis

Time window method uses a fixed window size and moves this window along the whole time series data at the speed of one time step for each moving

Time period	Window length
Odd	$(T + 1)/2$
Even	$(T + 1)/2 \pm 1/2$

Window 1:      Day 1   Day 2   Day 3

Window 2:              Day 2   Day 3   Day 4

Window 3:                      Day 3   Day 4   Day 5

# Window analysis

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**Aim:** to detect the trend in driving performance of each driver over time

**How:** The performance of a driver is assessed by treating it as a different driver in each time period

**Result** the performance of a driver in a particular period is contrasted with its own performance in other periods in addition to the performance of other drivers



# Window analysis of alternative n, with a 3-days window

First, in each window, the MLDEA-CI model should be applied to evaluate the relative performance of all the drivers under study

Driver	Period	Day1	Day 2	Day 3	Day 4	Day 5	Mean Index Score (M)	Variance (V)	Column Range (CR)	Total range (TR)
n	$W_1$	$I_{1,1}^n$	$I_{1,2}^n$	$I_{1,3}^n$						
	$W_2$		$I_{2,2}^n$	$I_{2,3}^n$	$I_{2,4}^n$					
	$W_3$			$I_{3,3}^n$	$I_{3,4}^n$	$I_{3,5}^n$				
	$CR_{n,t}$	x	$CR_{n,2}$	$CR_{n,3}$	$CR_{n,4}$	x	$M_n$	$V_n$	$CR_n$	$TR_n$

X: Omitted

# MLDEA-CI method

$$CI_0 = \max \sum_{f_1=1}^s \hat{u}_{f_1} y_{f_1 0}$$

The driver under evaluation

$$s.t. \quad \sum_{f_1=1}^s \hat{u}_{f_1} y_{f_1 j} \leq 1, \quad j = 1, \dots, n$$

All driver

$$\sum_{f_1 \in A_{f_k}^{(k)}} \hat{u}_{f_1} / \sum_{f_1 \in A_{f_{k+1}}^{(k+1)}} \hat{u}_{f_1} = w_{f_k}^{(k)} \in \Theta, \quad f_k = 1, \dots, s^{(k)}, \quad k = 1, \dots, K-1$$

$$\hat{u}_{f_1} \geq 0, \quad f_1 = 1, \dots, s$$

# Multiple Layer Data Envelopment Analysis- MLDEA model

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- The focus of DEA is on individual
- By solving the model, the best possible indicator weights are determined
- An index score between zero and one is obtained for each driver, with a higher value indicating a better performance
- Take into account the layered hierarchy of indicators that often exist in reality

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# Result

# Measuring driver's relative performance over time

Index scores of drivers using window analysis with a 3-days window

	Day1	Day 2	Day 3	Day 4	Day 5	Mean Index Score (M)	Variance (V)	Column Range (CR)	Total range (TR)
<b>Driver 3</b>									
<b>W<sub>1</sub></b>	0.9820	1	1			0.9926	0.0001	0.0084	0.0218
<b>W<sub>2</sub></b>		1	1	0.9782					
<b>W<sub>3</sub></b>			1	0.9867	0.9864				
<b>CR<sub>3,t</sub></b>	x	0	0	0.0084	x				
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
<b>Driver 7</b>									
<b>W<sub>1</sub></b>	0.7794	0.7520	0.7645			0.7654	0.0003	0.0234	0.0491
<b>W<sub>2</sub></b>		0.7520	0.7643	0.7394					
<b>W<sub>3</sub></b>			0.7860	0.7627	0.7885				
<b>CR<sub>7,t</sub></b>	x	0	0.0217	0.0234	x				

**Column views** show the stability of results at the same days

**Row views** show the trend of drivers' performance at different days

(X: Omitted)

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# Conclusion

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- DEA window analysis is a promising approach for driver performance evaluation
- It takes into account not only the multi-dimension of driving performance but also the variation in performance over time

## What to do next?

Investigate the validation of the results

Test other parameters/indicators such as the standard deviation of the lateral position instead of the absolute lateral position

Study the relationship between driving performance and other criteria such as workload

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**Thank you for your attention**

**Suggestions**

**Remarks**

**Questions?**

