



# A three-stage service network design model for intermodal transport under uncertainty

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## Digital twin for synchromodal transport

Partners:



Objective: Facilitate synchromodal transport

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Support logistics service providers in their transition towards synchromodal transport

“Synchromodal transport is **real-time, dynamic** and **optimised** intermodal transport” (Ambra et al., 2019)

How? Decision support model to assist capacity decisions under uncertainty

## Optimise capacity planning under uncertainty

### (1) Which capacity?

- Train slots on the long/medium term
- Trucking capacity in the short term

### (2) Which uncertainty?

- Demand volume
- Available train slots over time
- Train slot prices over time

# Network assumptions

## Train services

- Offered by rail operators
- LSPs can book slots between each terminal pair
- Fixed schedules
- Can be booked in advance

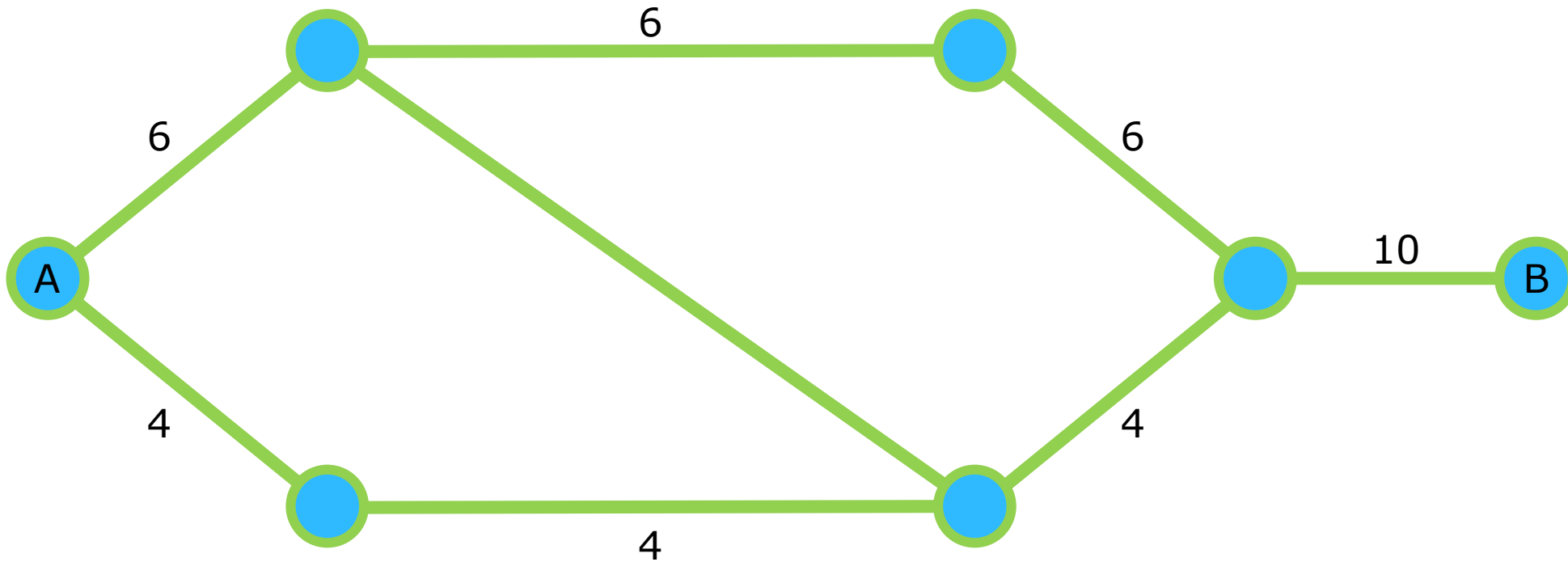
## Truck services

- Unlimited number
- More expensive and faster than trains
- Only booked in the short term

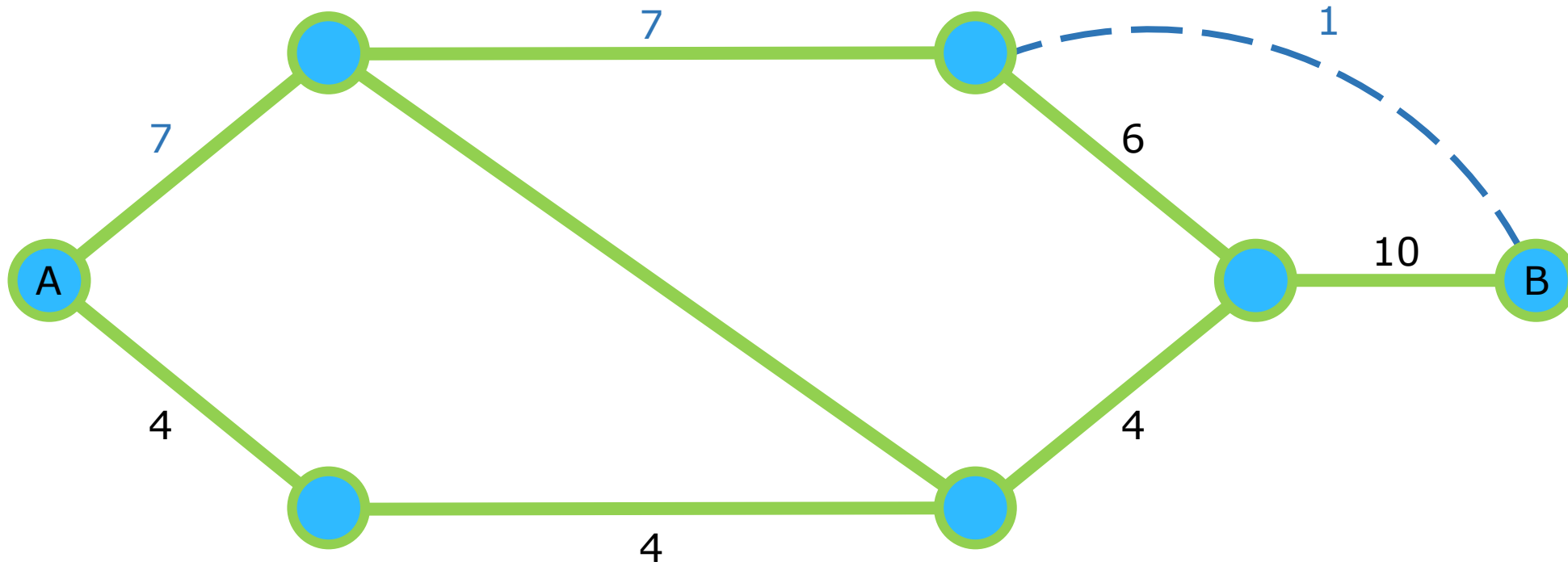
## Terminals

- Cost per transhipped container
- Transshipment time

# Network example



# Network example



# Literature results

Modelling approach	Capacity and transportation time	Demand	Demand and transportation time
Chance-constrained mixed integer programming			1
Fuzzy chance-constrained mixed integer programming	1		
Mixed integer linear program			1
Simulation optimisation			1
Two-stage chance constrained programming			1
Two-stage robust programming		1	
Two-stage stochastic programming		6	
<b>Total number of studies</b>	<b>1</b>	<b>7</b>	<b>4</b>



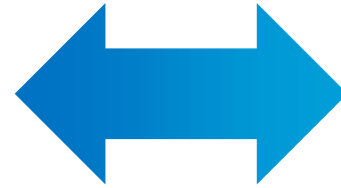
# Planning timeline

6 months

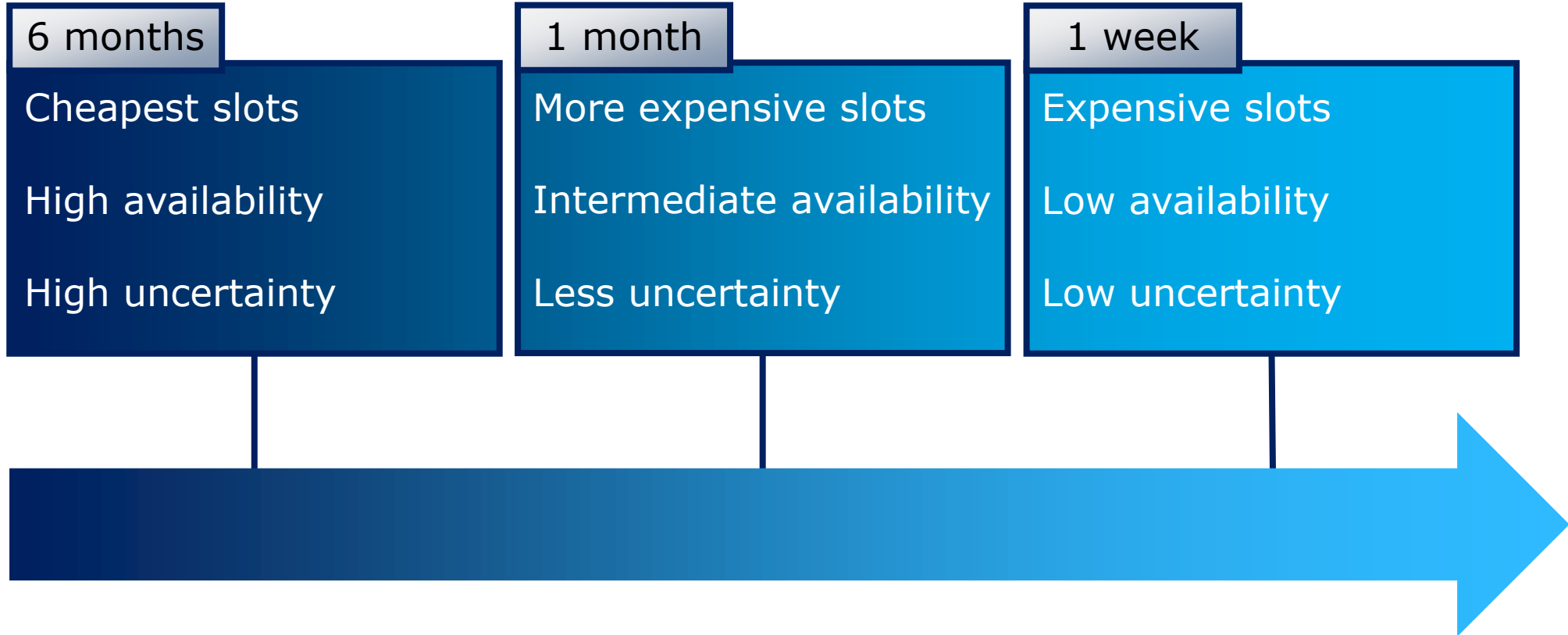
Cheapest slots  
High availability  
High uncertainty

1 week

Expensive slots  
Low availability  
Low uncertainty



# Planning timeline



## Integer programming model

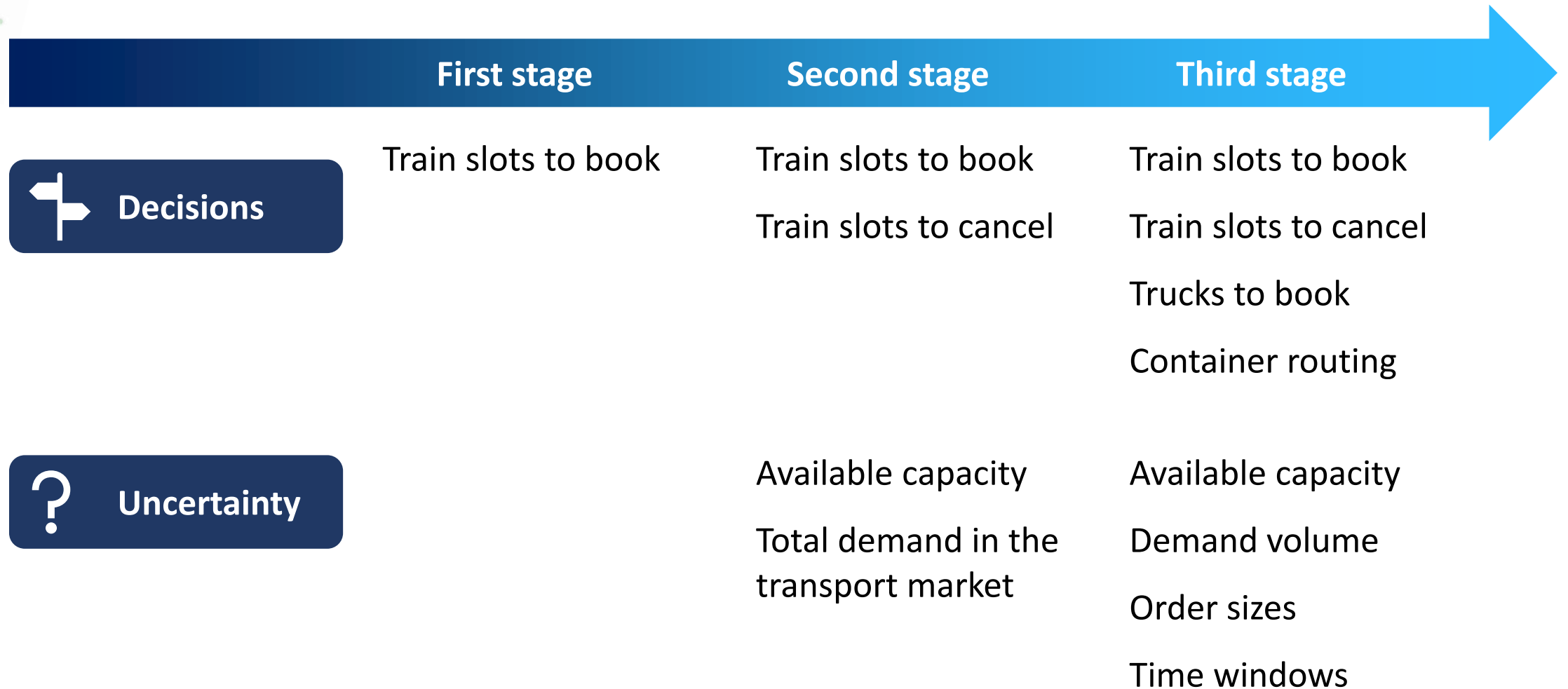


### Objective

Minimise costs

- Train slots at each stage
- Trucking at the operational stage
- Transshipment

# Model description





# Modelling uncertainty

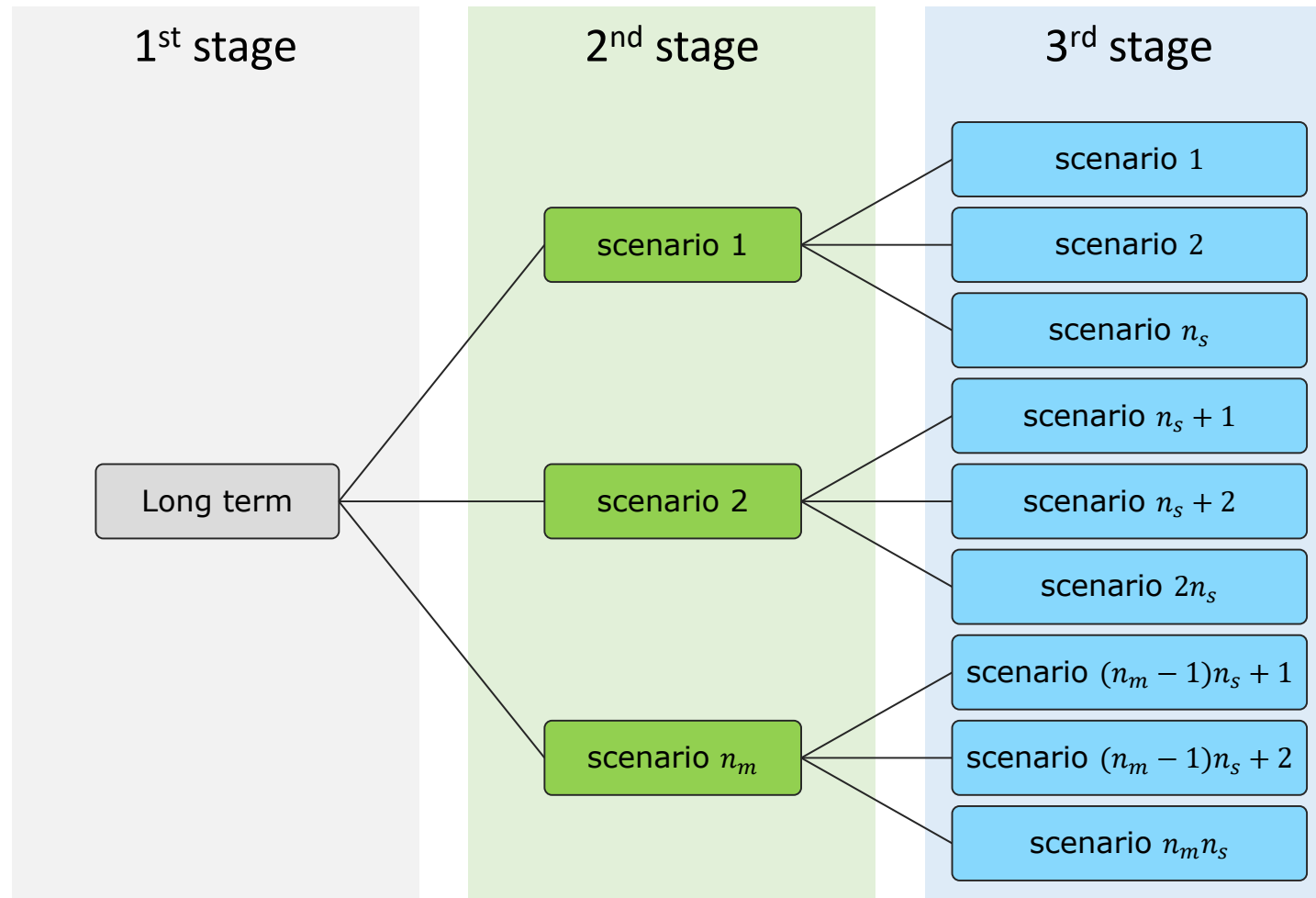
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How is demand modelled?

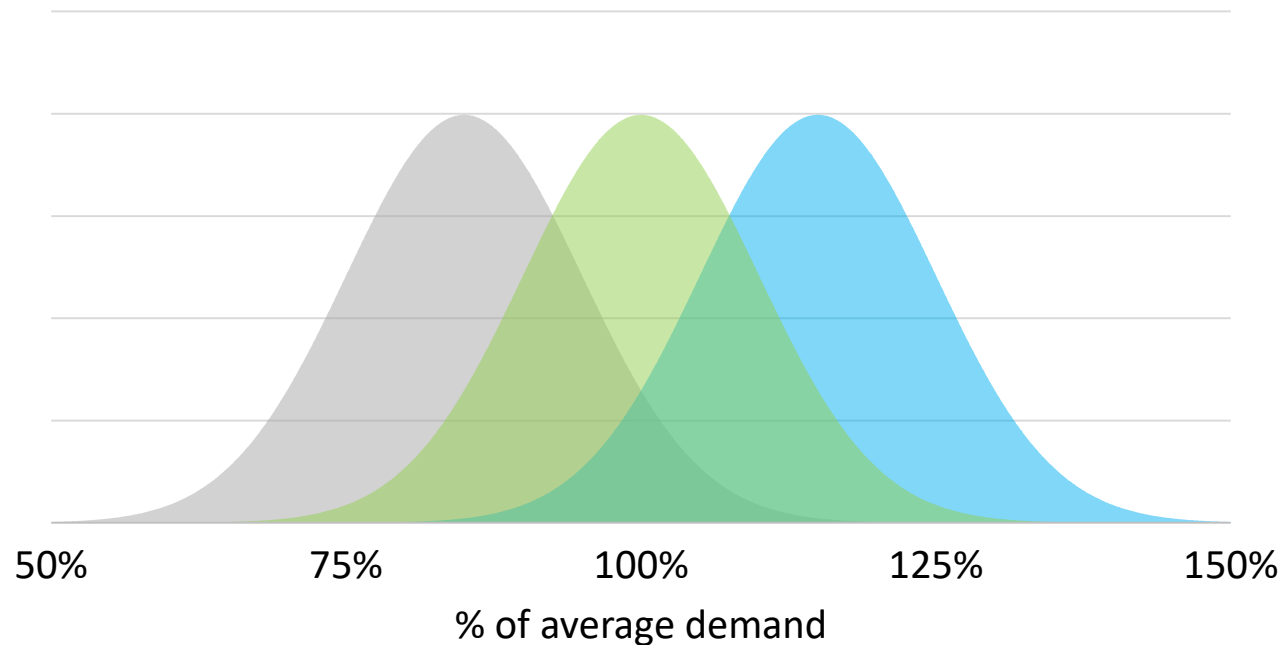
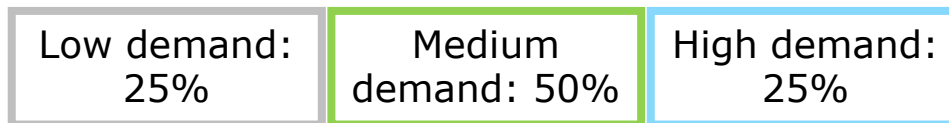
How many train slots are left at each stage?

What are the train slot prices at each stage?

# Scenario tree



# Demand modelling

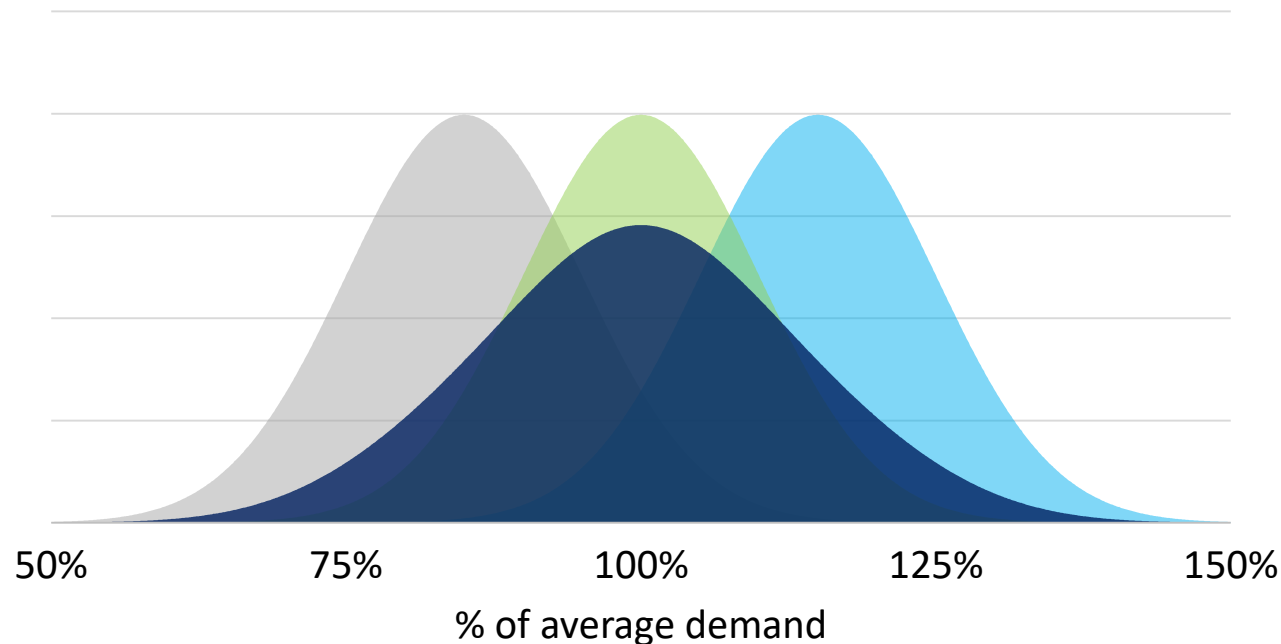
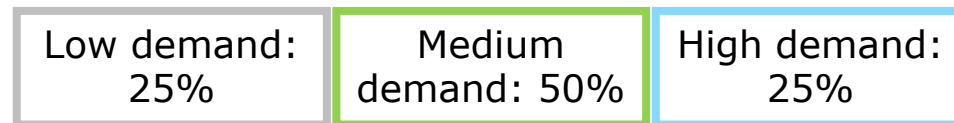


Each terminal pair has its own average demand

2<sup>nd</sup> stage demand distributions depend on the **total demand in the market**

Each market state has its own probability

# Demand modelling



Each terminal pair has its own average demand

2<sup>nd</sup> stage demand distributions depend on the **total demand in the market**

Each market state has its own probability

Long-term demand distribution is the weighted sum of the 2<sup>nd</sup> stage distributions

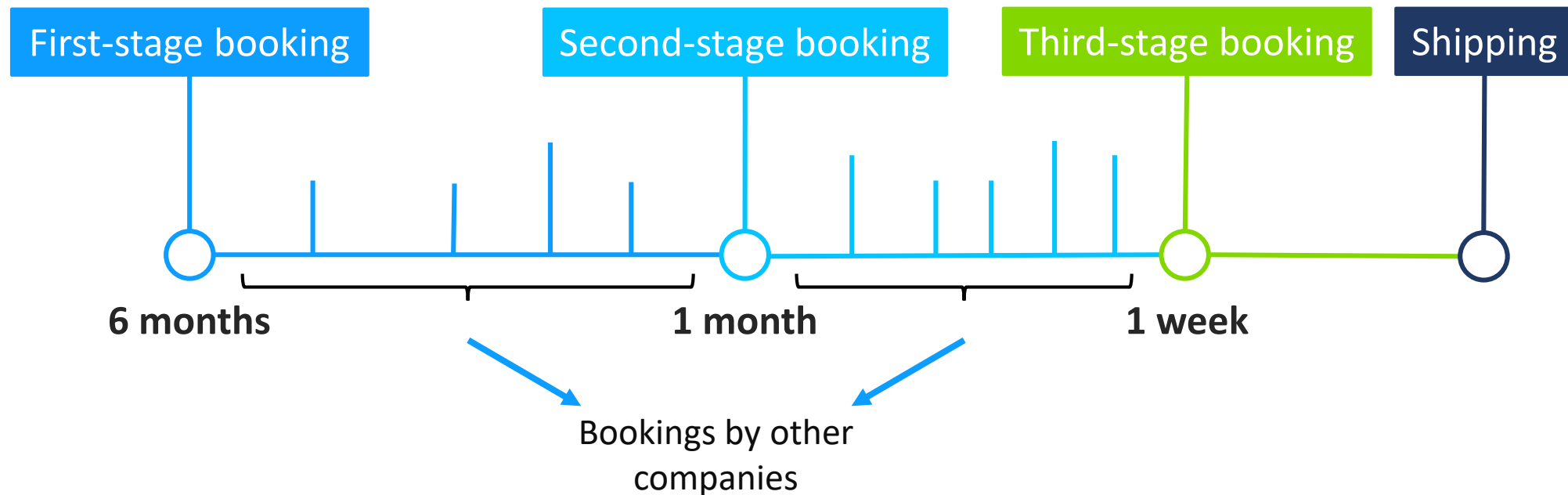


# Available number of train slots

Fixed in the first stage

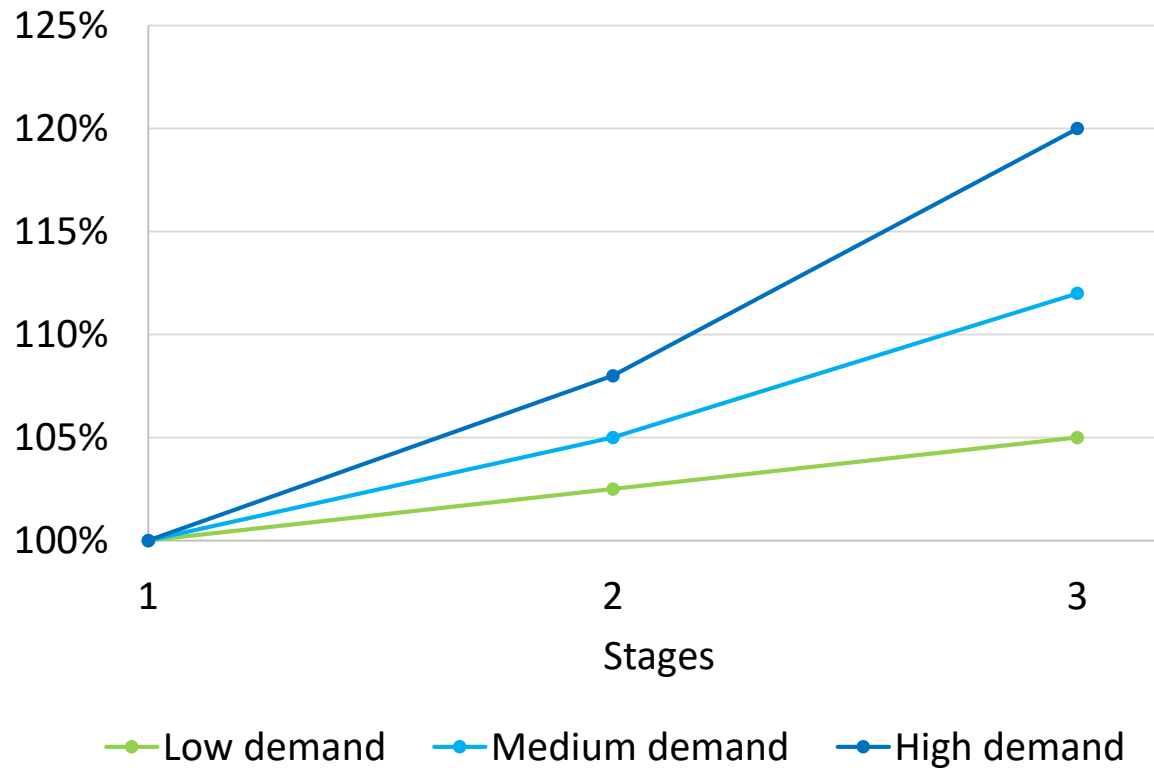
Second and third stages:

- Stochastic capacity decrease per connection
- Distribution mean depends on the market state



# Train slot prices

Evolution of prices per train slot



Fixed increase compared to initial prices

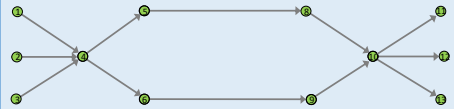
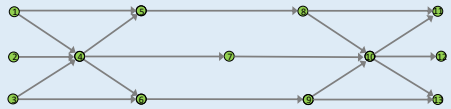
Depends on the market state

Exact commercial solver with a time limit

Sensitivity analyses:

- Fictional instances
- Comparison between 2-stage and 3-stage models
- Common random numbers to reduce variance

# Sensitivity analyses

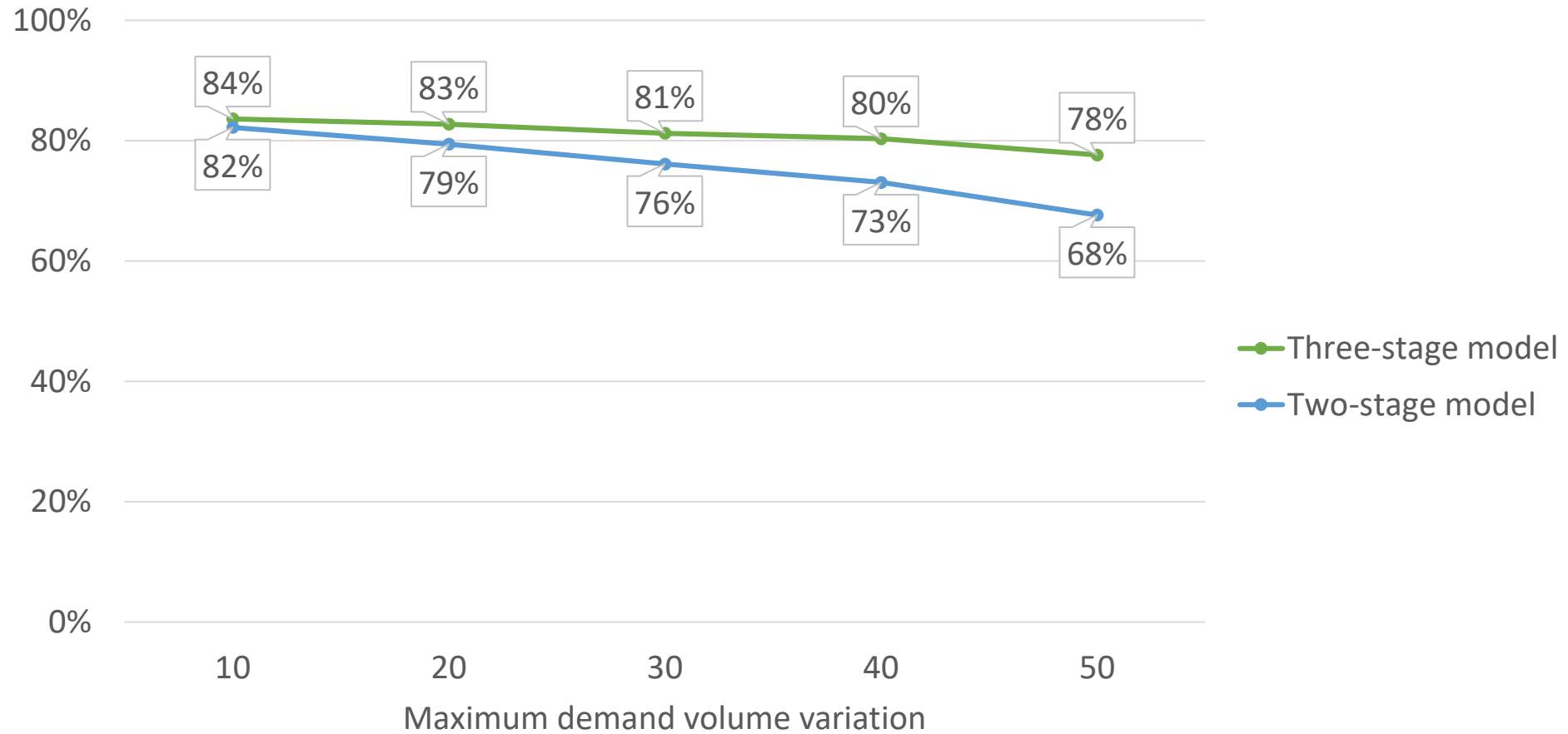
Network		
# train services	4	7
Capacity/demand ratio	1.2	1.7
Train/truck cost ratio	50%	75%
Demand volume variance	10%	50%

# Experimental results

Measure	2-stage model	3-stage model	Difference
Average cost	€ 430,100.75	€ 424,684.23	-1.26%
Average cost over lower bound	€ 25,616.90	€ 20,200.38	-21.14%
Average distance by train in km	267,558.0	284,578.3	6.36%
Average distance by truck in km	96,106.2	83,876.1	-12.73%

# Experimental results

Share of rail transport with varying demand volume variance



# Model contributions

More realistic compared to two-stage models in academic literature

Combination of stochastic demand and capacity

Better decision-making

What-if analyses

- Impact of demand uncertainty
- Effect of network changes
- Effect of other input parameters (truck/train cost ratio, demand volume/capacity ratio, prices, ...)

Thank you for your attention



Questions are welcome

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Research group website:

<https://www.uhasselt.be/en/onderzoeksgroepen-en/research-group-logistics>



# Literature results

REFERENCE	TRANSPORT MODES	STOCHASTICITY	APPROACH
Lium et al. (2009)	Unspecified	Demand	Two-stage stochastic programming
Hoff et al. (2010)	Unspecified	Demand	Two-stage stochastic programming
Crainic et al. (2011)	Unspecified	Demand	Two-stage stochastic programming
Bai et al. (2014)	Unspecified	Demand	Two-stage stochastic programming
Meng et al. (2015)	Barge, rail, road	Demand	Two-stage stochastic programming
Demir et al. (2016)	Barge, rail, road	Demand and transportation time	Mixed integer linear program
Layeb et al. (2018)	Barge, rail, road	Demand and transportation time	Simulation optimisation
Sun et al. (2018)	Rail, road	Capacity and transportation time	Fuzzy chance-constrained mixed integer programming
Zhao et al. (2018)	Rail, ship	Demand and transportation time	Two-stage chance constrained programming
Zhao et al. (2018)	Rail, ship	Demand and transportation time	Chance-constrained mixed integer programming
Wang and Qi (2019)	Unspecified	Demand	Two-stage robust programming
Wang et al. (2019)	Unspecified	Demand	Two-stage stochastic programming